Design, implementation and modelling of the single and multiple extensor pneumatic muscle actuators

Al-Ibadi, Alaa, Nefti-Meziani, S and Davis, ST

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Design, implementation and modelling of the single and multiple extensor pneumatic muscle actuators

Alaa Al-Ibadi, Samia Nefti-Meziani and Steve Davis

Abstract
The soft actuator represents a valuable addition to the robotics research area in last two decades. These actuators provide significant features such as lightweight, softness, high force to weight ratio and the ability to form in different shapes. This article presents a new length model to the single extensor pneumatic muscle actuator (PMA) which is depended on the constructed parameters and the air pressure. On the other hand, the tensile force formula of the contractor actuator has been modified to describe the extension force of the extensor PMA. The parallel structure of four extensor actuators is designed and implemented as continuum arm. The bending behaviour of the proposed arm is illustrated and modelled mathematically. The length model of the single extensor actuator has validated by the comparison between the model and the experiment data and then a neural network (NN) control system is applied to control the elongation of the extensor PMA. The kinematics for the proposed continuum arm are presented to describe the bending of the arm and its direction.

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Keywords
Extensor pneumatic muscle actuator; extension force; extensor continuum arm; kinematics; neural network controller

1. Introduction
Soft actuators have grown commonly reputation among researchers, mainly in the last two decades. As a result, soft robotics has been extensive use in the numerous areas. Researchers from different fields such as material science, biology and computer and control engineering interest in such type of robots (Margheri & Trimmer, 2014). This developing research field emphasises on robots made of soft materials which increase the safety of human-robot interaction, and make the robot more compliance to its environment (Mutlu, Yildiz, Alici, Marc in het Panhuis, & Spinks, 2016; Pillsbury, Guan, & Wereley, 2016). The infinite number of freedom (DOF) is achievable by soft robots due to the bending capability of the soft actuator and as a result, a robot end effector can reach every point in the 3D workspace (Trivedi, Rahn, Kier, & Walker, 2008). Soft robots have a further positive over rigid robots, where they produce slight resistance to obstacles and can adapt to them. Consequently, soft and fragile payloads could be handled without causing any damages (Jones & Walker, 2006).

A pneumatic muscle actuator (PMA) which is built from an inner rubber tube bounded by a braided sleeve (Chou & Hannaford, 1996) has been used to create soft robots. The construction of the PMA defines the type of actuator, by selecting the length of both the inner tube and the braided sleeve the PMA act as a contraction actuator if the braided angle is less than 54.7° (Al-Ibadi, Nefti-Meziani, & Davis, 2016; Godage, Branson, Guglielmino, & Caldwell, 2012), and the extension actuator if the angle is more than 54.7° (Al-Ibadi, Nefti-Meziani, & Davis, 2017b). Moreover, the PMA will produce a tensile force for contractor type and an extension force for the extensor PMA.

Important researches have been done to define the contraction force of the pneumatic muscle actuators. Among these researches, the Chou and Hannaford model (Chou & Hannaford, 1996) and Tondu and Lopez (2000) is commonly referred. Several modifications and new models are presented to these formulas in order to reduce the error and to consider all the actuator parameters. Davis and Caldwell (2006) study the impact of the braided sleeve on the tensile force. Al-Ibadi, Nefti-Meziani, and Davis (2017a) formulate a model of the contraction force by considering the specifications of the inner rubber tube and the actuator dimensions.

Hannan and Walker (2003) designed a rigid material continuum robot arm inspired by an elephant trunk, which has the ability to bend in constant curvature by tendons. Bailly and Amirat (2005) implemented and controlled two sections continuum robot for surgical application to enhance the bending behaviour.
Several soft prototypes have been designed to achieve a unique application such as OctArm by McMahan et al. (2006) which is flexible, elastic and has good strength, but is complex to build and control because of the multiple pressurized central members that make the design mechanically challenging. The Air-Octor continuum arm by McMahan, Jones, and Walker (2005) on the other hand, is much less complex to build and control because of the single central member and the use of cables as actuators but lacks flexibility and strength due to high cable friction which cannot be overcome by low pressure in the central member, resulting in cable binding which in turn causes undesirable movements of the trunk.

Another design has been implemented by Neppalli and Jones (2007) by using single extensor pneumatic actuator and three cables to arrange the direction of the free end. This design provides bending in an arc of constant curvature and it is easy to control by motors, and it can work with an air pressure up to 483 kPa. However, they do not provide any data about the load condition and the grasping performance for the presented soft arm.

Several types of controller systems have been used to control the single contraction pneumatics actuator. Ahn and Nguyen (2007) designed a PID controller to control the length of the contractor actuator for three different loads (0, 5 and 10 kg). Andrikopoulos, Nikolakopoulos, and Manesis (2014) proposed an advanced nonlinear PID (AN-PID) controller by adding nonlinear elements to the conventional PID to enhance the control system due to the high nonlinearity of the PMA performances. Fan, Zhong, Zhao, and Zhu (2015) presented a nonlinear PID controller tuned by a back propagation neural network (BP-NN).

In this article, different lengths of the extensor PMAs have been constructed to study their performances. A novel model of the elongation is presented and validated by comparing the model result with the experimental data and a NN control system is applied to control the actuator length and validate the elongation formula. The load effect on the actuator length is illustrated in section five. In section six, a continuum arm of four extensor actuators is designed and its bending behaviour is illustrated. While the kinematics for the bending performances is giving in section eight.

2. The extensor PMA

The construction of the PMA defines its action as a contraction or extension actuator by controlling the braided angle (θ); as identified in the force formula below, the force either contraction or extension depends on (θ). A photograph of a 30 cm extensor PMA is shown in Figure 1. Generally, the PMA is constructed from an inner rubber tube which is covered by a braided sleeve with two solid material terminals which are fixed strongly to ensure that no air leakage occurs. One of the terminals has a small inlet for the actuated air. Figure 2 shows a basic diagram of PMA with ‘L’ length, ‘D’ diameter and ‘θ’ angle between the vertical axis and braided strand (b).

When the length of the braided sleeve is more than the length of the rubber inner tube in sufficient amount in which the braided angle (θ) is more than 54.7° (Liu & Rahn, 2003), the actuator behaviour is an extensor PMA. In this project, the braided sleeve length is 2.8 times of the inner tube. The percentage of extension differs from one muscle to another, and it is up to 50% (McMahan et al., 2006).

3. The elongation model of the single extensor actuator

To formulate an elongation mathematical model of single extensor PMA, three actuators in different initial lengths
Table 1. The initial specifications of the extensor PMAs.

<table>
<thead>
<tr>
<th>$L_0$ (m)</th>
<th>Rubber thickness (m)</th>
<th>Braided thickness (m)</th>
<th>Inner diameter (m)</th>
<th>Rubber stiffness (N/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2</td>
<td>$1.1 \times 10^{-3}$</td>
<td>$0.5 \times 10^{-3}$</td>
<td>$12 \times 10^{-3}$</td>
<td>363.33</td>
</tr>
<tr>
<td>0.3</td>
<td>$1.1 \times 10^{-3}$</td>
<td>$0.5 \times 10^{-3}$</td>
<td>$12 \times 10^{-3}$</td>
<td>363.33</td>
</tr>
<tr>
<td>0.4</td>
<td>$1.1 \times 10^{-3}$</td>
<td>$0.5 \times 10^{-3}$</td>
<td>$12 \times 10^{-3}$</td>
<td>363.33</td>
</tr>
</tbody>
</table>

Figure 3. The elongation and $t$. (L$_0$) are designed and built. Actuators of (20, 30 & 40 cm) are chosen to cover a range of muscle lengths; all these muscles have the same initial diameter of (3.3 cm) and an initial braided angle of (71.5°). The material specifications of the constructed actuators are specified in Table 1.

The experiment is done by applying an air pressure via (3/3 matrix solenoid valve) for steps start from 0–500 kPa. And an ultrasound HC-SR04 sensor has been attached to the end of the actuator to calculate the change in the length. An Arduino mega 2650 is used to control the experimental process. The experiment is repeated several times to each actuator and the length of each PMA is recorded during the elongation (increasing the applied pressure) and the contracting (decreasing the applied air pressure). The results as a function of air pressure are shown in Figure 3.

Figure 4 illustrates the average length of each actuator, which represents the average between the elongation and the contraction. The sigmoidal shape of muscle length leads to modelling the length of PMA performance as a mathematical sigmoid function.

The average length of each actuator is presented as a sigmoid function individually, then, the three equations combined in one new formula depends on both the air pressure and the initial length as in (1) and (2). The parameters of (2) have been found by curve fitting the parameters of the sigmoidal function of different actuators lengths.

$$L = a - \frac{b}{1 + \left(\frac{p}{c}\right)^d} + 0.0009L_0p^2,$$  \hspace{1cm} (1)

$$\begin{bmatrix} \begin{array}{c} a' \\ b \\ c \\ d \end{array} \end{bmatrix} = \begin{bmatrix} 0.2281 & 0.084598 & -0.0013189 \\ -0.94047 & 0.095934 & -0.0014863 \\ 0.014934 & 0.0012083 & -0.000026277 \\ 0.2080174 & -0.0032043 & 0.0000106189 \end{bmatrix} \times \begin{bmatrix} L_0 \\ L_0^2 \\ L_0^3 \end{bmatrix}.$$  \hspace{1cm} (2)

The extension ratio for the extensor PMA can be defined as in (3):

$$\varepsilon' = \frac{L - L_0}{L_0}.$$  \hspace{1cm} (3)

Figure 5 shows the average length of the PMAs for both the experimental and the model data, and it is clear that there is a significant matching between the two plots for different sets of data.

To validate this formula another actuator has been constructed for the same specifications but with 25 cm initial length.

Figure 6 illustrates both the experimental and model length characteristics for the new muscle, which it proved the validity of the extensor length formula in (1) and (2).
4. Controlling the actuator length

A neural network (NN) controller is designed by Matlab to control the length of single extensor PMA by controlling the air filling and venting of the actuator via a 3/3 solenoid (Matrix) valve and an Arduino Mega 2560. Figure 7 shows the flowchart of the control system and the extensor actuator, the attached load and the ultrasound sensor are illustrated in Figure 8. The NARMA-L2 NN-controller is used of 9-neurons in one hidden layer, 3-delayed plant inputs, 2-delayed plants outputs and it is trained by (trainlm) for 100 Epochs. The mean square error (MSE) for the training, testing and validating data is about $10^{-7}$. The controller output is the pulse width modulation (PWM) signal which controls the air flow for both the filling and the venting processes to achieve the desired length.

An approximate model has been used to train the neural controller and the actuator length as a function of the duty cycle of the controlled input is given by (4).

$$L = L_0 + \frac{0.5L_0 \times u}{98}, \quad (4)$$

where $L$ is the actuator length and $u$ is the controlled duty cycle of the pulse width modulation (PWM) signal. $L_0$ represents the initial length, the number (98) refers to the 98% of the maximum duty cycle for the control signal to avoid continues supply to the air valve, and 0.5 is referring to the average extension ratio (50%) of the extensor PMA.

(4) is found by applying different values of the duty cycle for one second then recording the actuator length by the ultrasound sensor.

A step signal is applied to the controller system at 0.5 Hz, and the step response for the elongation process is illustrated in Figure 9.

Figure 9 shows that the contracting time is more than the elongation time because of the hysteresis of the actuator material. The air pressure of the extensor PMA is recorded during the controlling process and it is applied to the modelling formula in (1) and (2) in order to further validation of the proposed length model. The result of this validation is illustrated in Figure 10 and it shows

![Figure 6](image_url)  
**Figure 6.** The validation data for the 25 cm extensor actuator.

![Figure 7](image_url)  
**Figure 7.** The flowchart of the connections among the PC, Arduino, Solenoid valve, and the extensor actuator.

![Figure 8](image_url)  
**Figure 8.** The extensor PMA at different attached load and the position of the ultrasound sensor.
Figure 9. The step response of the 30 cm extensor actuator at 0.5 Hz.

Figure 10. The step input and the model length of the 30 cm extensor actuator.

Figure 11. The geometrical analysis of the PMA.

Figure 12. The experimental force data with the plot of (9) for the 30 cm PMA. This figure illustrates that the difference between the theoretical and experimental records has two main causes. The first one is the non-cylindrical shape of the PMA at zero or low applied air pressure. The second reason is that there is no perfect contact between the inner rubber tube and the braided sleeve and the resistance of rubber tube (Al-Ibadi et al., 2017a). To overcome these two aspects, the correction factor \( q(p) \) is used and the force formula can be modified as in (11).

\[
q(p) = -(1 + e^{-0.5p}).
\]

The increasing in gauge pressure caused an increase in the correction factor, therefore, at high pressure; the shape of the PMA becomes perfectly cylindrical. On the other hand, the experimental data shows that the amount

5. Modelling of the extension force

The PMA converts the air energy into mechanical form by transferring the pressure input to the muscle into the extensor force. Referring to the virtual work theory, the varying of input work \( (w_{\text{in}}) \) of the pneumatic muscle is

\[
dw_{\text{in}} = p.dv,
\]

where \( (dv) \) is the volume change of the actuator. The output work \( (w_{\text{out}}) \) changes with the change of length, as in the following equation:

\[
dw_{\text{out}} = f.dL.
\]

Figure 11 shows the relation between the parameters of the PMAs. Equations (7), (8) and (9) define the Tondu and Lopez force model under the following assumptions: 1- The shape of the PMA is a perfect cylinder with zero wall thickness. 2- There is a contact between the inner rubber tube and the braided sleeve. 3- The braided strand length is constant. 4- There is no friction between the tube and

where \( b \) is the strand length and \( n \) is the number of strand turns. By considering (7) the strand length can be evaluated as:

\[
b = (L^2 + (Dn\pi)^2)^{1/2}.
\]

The extension force \( f \) can be calculated as the multiplication of the gauge pressure and the volume change with respect to length.

\[
f = -\pi r_0^2 p(\alpha(1 - \varepsilon')^2 - \beta),
\]

where \( \alpha = \frac{3}{\tan^2(\theta_0)} \) and \( \beta = \frac{1}{\sin^2(\theta_0)} \), \( \varepsilon' \) is the extension ratio for the extensor PMA.

Moreover, \( r_0 \) and \( \theta_0 \) represent the initial values of radius and the braided angle of the PMA respectively.

Where from Figure 11:

\[
L = b \cos \theta, \quad D = b \frac{\sin \theta}{n\pi},
\]

where \( b \) is the strand length and \( n \) is the number of strand turns. By considering (7) the strand length can be evaluated as:

\[
b = (L^2 + (Dn\pi)^2)^{1/2}.
\]

The increasing in gauge pressure caused an increase in the correction factor, therefore, at high pressure; the shape of the PMA becomes perfectly cylindrical. On the other hand, the experimental data shows that the amount

the sleeve. 5- Neglecting the latex tube force (Tondu & Lopez, 2000).

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L = b \cos \theta, \quad D = b \frac{\sin \theta}{n\pi},
\]

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\[
q(p) = -(1 + e^{-0.5p}).
\]

The increasing in gauge pressure caused an increase in the correction factor, therefore, at high pressure; the shape of the PMA becomes perfectly cylindrical. On the other hand, the experimental data shows that the amount
of (zero force) pressure is (45 kPa). Due to the resistance of inner tube against the stretch and the contactless between the braided sleeve and the inner tube, the energy of actuated air below 45 kPa will be considered as loses, for that the extensor force in (10) is defined to be (0 N) from (0–45 kPa) and the gauge pressure shift by (45 kPa) otherwise. The zero force pressure is studied by Tsagarakis and Caldwell (2000) as a function of pressure and inner tube diameter. Here, it is found that this constant value could be considered for this type of PMAs.

Taking these two factors into account gives substantial matching between the experimental and theoretical force characteristics. The force of all actuators under study has been validated and Figure 13 gives the force plot for the (30 cm) PMA.

The modification of (10) shows in (11) below:

\[
 f = 0, \quad 0 \leq p \leq 45 \text{ kPa},
\]
\[
 f = -\pi r^2_o (p - 45)[\alpha (1 - q\varepsilon')^2 - \beta], \quad p \geq 45. \tag{11}
\]

6. Load effects on actuator behaviour

Attaching load to the extensor PMA changes its extension ratio. Figure 14 shows the length of the actuator with respect to the attached load at gauge pressure (100–500) kPa. Increasing the attached load gives the PMA more ability to extend at low pressure (\( p \)). In this figure, all lines intersect around (3.5) kg.

The load test is done as follows: a- Attached different loads up to 10 kg in 0.5 kg steps at 100 kPa. b- Increase the pressure to 500 kPa in 50 kPa steps and repeat step (a) each time. Figure 15 shows that the behaviour of the muscle is changed after load 3.5 kg, where increasing the gauge pressure makes the PMA act as a contraction instead of an extension muscle.

From Figures 14 and 15, the extensor muscle might be used as a contractor actuator when it is loaded with more than 3.5 kg.

As mentioned in section 2 above, when the braided angle is more than 54.7°, the actuator acts as an extensor muscle. On the other hand, it works as a contractor muscle when (\( \theta \)) is less than 54.7°. The high angle occurred as a result of the long braided sleeve compared with the inner tube. In this paper (2.8 times) of braided sleeve longer than the inner tube has been used. The elasticity characteristic of the rubber tube gives the muscle a capability of elongation under the load effect, making (\( \theta \)) less than the threshold value. As a result, the actuator behaviour changes to contraction. This performance provides an additional advantage for the extensor PMA and makes it able to extend first at a certain pressure at no load then carries a certain weight then pick up it at high pressure.
7. Extensor continuum arm

The traditional way in which PMAs are used is to produce a linear contraction or extension. However, this section explores using the extensor actuator in such a manner that when activated, it bends.

McMahan et al. (2006) explain that using the principle of the constant-volume creates the bending behaviour of the extensor PMA, where the dimensional adjustment on one side leads to a dimensional modification on another side.

To achieve the bending behaviour for the extension PMA, a high-tension thread is used to fix one side of the actuator, which prevents it from extending, while the other sides are free to elongate. The whole muscle will bend toward the thread side when pressurized. Figure 16 shows a 30 cm extensor actuator and how it bends at 300 kPa air pressure. The air pressure has been applied gradually from zero to 500 kPa through a solenoid valve and the bending angle is recorded by the MPU 6050 sensor. The maximum bending angle for the single extensor actuator is about 450° at 500 kPa at the no-load condition and the maximum bending payload is 2.0 kg.

To develop the bending in all directions a 4-PMAs continuum arm is designed and constructed as shown in Figures 17 and 18. Four extension actuators 30 cm each are used; one in the centre and the others are located at 3 cm from the centre and 120° between each other.

A Solidworks 2015 is used to design the two ends, and a 3D printer is used to print them. Then the centre actuator is connected to others individually. Equal air pressure in all PMAs makes the arm extend in a straight direction, while, the different pressure inside the four actuators make the free end move in all direction in the space at almost constant curvature (Walker, 2013). The position angle is observed as a function of the supplied pressure and the attached load.

Firstly, the experiments are done by recording the initial angle of the free end (δ), which it is equal to (zero)
degree due to a straight-line arm. Secondly, all PMAs are actuated by (45 kPa), then the pressure is increased in one of the PMAs in the corner. The arm will then bend into another position, depending on the amount of the pressure in the muscle. And $\delta$ is recorded each time. Figure 19 shows the extension arm under actuation of 300 kPa.

The maximum angle value ($\delta_{\text{max}}$) depends on the amount of the attached load ($w$) to the arm end. Table 2 below shows different maximum angles with different load values.

The bending angle against the air pressure at different load values is illustrated in Figure 20 which it represents the position of the free end at any pressure step.

### Table 2. Maximum angle at different loads.

<table>
<thead>
<tr>
<th>Load $w$ (kg)</th>
<th>Pressure $P$ (kPa)</th>
<th>$\delta_{\text{max}}$ (degree)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>500</td>
<td>164.83</td>
</tr>
<tr>
<td>0.1</td>
<td>520</td>
<td>163</td>
</tr>
<tr>
<td>0.2</td>
<td>500</td>
<td>155</td>
</tr>
<tr>
<td>0.3</td>
<td>520</td>
<td>135.2</td>
</tr>
<tr>
<td>0.4</td>
<td>500</td>
<td>126.1</td>
</tr>
<tr>
<td>0.5</td>
<td>500</td>
<td>116.2</td>
</tr>
</tbody>
</table>

From these data, the bending angle increase when the applied pressure increase and its value at each air pressure step depends on the attached load. In our experiment, various loads from 0 to 0.5 kg are attached. Furthermore, the arm starts to bend when the air pressure reaches 80 kPa and the angle has a fixed value ($\delta_{\text{max}}$) over 520 kPa. As a result, the operation range will be at pressure values from 80–520 kPa.

A new formula of the proposed extensor soft arm bending angle (12) is presented as a function of the input air pressure and the amount of attached load as follows:

$$\delta = a - \frac{b}{1 + \left(\frac{P}{c}\right)^d}$$

where

$$\begin{bmatrix} a \\ b \\ c \\ d \\ e \end{bmatrix} = \begin{bmatrix} 173.57 \\ -350.13 \\ 9014 \\ -172.1 \\ 312.6 \\ -8667.6 \\ 0.5798 \\ 2.2097 \\ -33.363 \\ 303.74 \\ -5310.1 \\ 36922 \\ 0.0045 \\ -0.0727 \\ 6.4529 \\ -62973 \\ 167422 \\ -148110 \\ 61529 \\ -164591 \\ 145972 \\ 201.17 \\ -499.34 \\ 431.94 \\ -118935 \\ 183790 \\ -111871 \\ -43.867 \\ 103.32 \\ -81.375 \end{bmatrix} \begin{bmatrix} 1 \\ w \\ w^2 \\ w^3 \\ w^4 \\ w^5 \end{bmatrix}$

Equation (12) above gives the bending angle at any air pressure amount from 0–600 kPa, while, the value of the parameters (a, b, c, d and e) depends on the attached load. The parameters of (12) have been found by curve fitting the parameters of the bending angle at each single load to generalised the bending angle formula for the proposed extensor continuum arm.

This formula is validated for all load conditions and Figure 21 gives the validation results for three conditions (0, 0.2 and 0.5 kg). This figure shows a significant matching between the experimental results and the presented formula.

### 8. Kinematics of the extensor continuum arm

The bending direction of the proposed arm depends on which extensor actuator is activated. Figure 22 shows the geometrical analysis of the actuators positions and the bending directions.

From Figure 19 the bending of the first extensors actuator is according to (12) and the direction of this bending
The validation results for the bending angle at three different load conditions.

Figure 22. The geometrical analysis of the extensor continuum arm.

is in the direction of the positive Y-axis (i.e. the extensor continuum arm will bend towards 90°). The bending due to the first actuator can be written as: \( \delta_1 \angle 90^\circ \). Similarly, the bending angles of the second and third actuators are defined as: \( \delta_2 \angle 330^\circ \) and \( \delta_3 \angle 210^\circ \) respectively. And the resultant bending angle of the arm can be defined as:

\[
\delta \angle \theta = \delta_1 \angle 90^\circ + \delta_2 \angle 330^\circ + \delta_3 \angle 210^\circ, \tag{13}
\]

where \( \delta_1, \delta_2 \) and \( \delta_3 \) are the bending angles of the soft arm due to the pressurized condition of the actuators 1, 2 and 3 respectively, and they calculated according to (12). The bending angle \( \delta \) of the proposed extensor continuum arm in the direction of \( \theta \) can be found anytime by applying (13).

Figure 19 shows three operation zones, each one represents the operation area for two actuators. The presented arm covers (zone1) when the actuators 1 and actuator 3 are activated. Similarly, pressurizing actuators 1 and 2 cover (zone2), and (zone3) is covered by actuators 2 and 3. Consequently, pressurizing the three actuators by different air pressure values makes the continuum arm moves to any of these zones according to (13).

9. Conclusion

This article presented full descriptions of design and implementation of the single extensor pneumatic muscle actuator. The elongation performance of this actuator is explained for different sizes. Then a novel mathematical model is proposed and validated by different sets of data and a neural network control system.

On the other hand, the load effect is explained by attaching different load values to the actuator. This experiment shows that the actuator behaviour converted to the contraction at 3.5 kg due to the decreasing in the braided angle. The experimental data gives the capability to use the extensor actuator as a contractor at a specifically attached load. This ability makes this type of PMA appropriate for multiple purposes.

The extension force for the extensor PMA is presented according to its structure taking into account the needed amount of air pressure to develop the force.

An extensor arm is built from four extensor PMAs and we studied its behaviour for bending. The experiments show high bending angle at load up to 0.5 kg. A formula for this bending angle is presented for no-load and load conditions. The validation of this formula shows a significant accuracy for the air pressure more than 80 kPa.

The kinematics for the presented soft arm is explained by the bending angle and its direction for any pressurizing conditions.

As a future work, a control system might be applied to the extensor soft arm to control the bending angle of the arm and its direction.

Disclosure statement

No potential conflict of interest was reported by the authors.

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