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# SHEAR BEHAVIOUR OF LIGHTWEIGHT CONCRETE BEAMS STRENGTHENED WITH CFRP COMPOSITE

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## ABSTRACT

This paper presents the experimental results obtained from lightweight and normal concrete beams with closed and U-shaped configurations of epoxy bonded Carbon FRP (CFRP) reinforcement in order to compare the shear resisting mechanisms between lightweight and normal concrete beams. The experimental results show that the CFRP can successfully be applied in the strengthening of lightweight concrete beams and the shear strength gained due to CFRP reinforcement for lightweight samples is less than the normal weight concrete samples while the mode of failures are the same. In contrast, diagonal shear cracks propagate through the lightweight aggregate compared to cracks around normal aggregate in the concrete matrix. Furthermore, the numerical study shows that the design guidelines to estimate the CFRP contribution, which do not differentiate the concrete types, overestimate the U-shaped CFRP contribution on lightweight concrete beams where the effective bond length of CFRP could not be achieved due to lower tensile strength of lightweight concrete.

Keywords: Buildings, structures & design; Composite structures; Concrete structures.

## List of Notations

$A_f$	Area of CFRP strap
$E_f$	Modulus of elasticity of CFRP strap
$\epsilon_f$	Strain on CFRP strap
$V_f$	Shear resistance by CFRP straps
$V_t$	Total shear capacity
$V_c$	Shear resistance by concrete

## 24 INTRODUCTION

25 Lightweight aggregates, Pulverised Fuel Ash (Lytag, 2011), instead of coarse granite  
26 aggregates have been used in concrete structural elements. The dead weight of concrete  
27 elements are significantly reduced due to lightweight aggregate and the geometric shape of an  
28 element cast with lightweight concrete can be increased without increasing its weight. In the  
29 coming decades, it is, therefore expected that structures constructed using lightweight  
30 concrete will occupy a significant proportion of concrete infrastructures.

31 Lightweight concrete structures are worse affected by deterioration than normal weight  
32 structures. This is due to permanent deterioration of concrete materials, applied load more  
33 than envisaged design load and lack of understanding in behaviour of lightweight concrete as  
34 a structural material. The deteriorated lightweight concrete structures may be retrofitted to  
35 reduce the economic impact rather than replace with new structures. Thus, recent studies as  
36 recommended in ACI 440.2R (2008) have been directed to investigate efficient strengthening  
37 systems such as near surface mounted and epoxy bonded steel or FRP reinforcements in  
38 lightweight concrete structures.

39 Shear failure in normal concrete is a controversial topic among structural engineers (Kim and  
40 Sebastian, 2002; Sundaraja and Rajamohan, 2009; Zhang, 1997; You et al., 2017). This  
41 disparity is because the different design guidelines suggest various relative contribution of  
42 shear carrying mechanisms such as aggregate interlock, friction between the shear cracks,  
43 dowel action by longitudinal reinforcement, and contribution to the compression zone and  
44 vertical resistance by shear links. Hence, there is no single universal design method accepted  
45 in different parts of the world. When it comes to retrofitted systems with FRP, variability in  
46 materials and bond properties add to the complication in design guidelines. This problem is  
47 further amplified due to the lack of aggregate interlock and weaker tensile strength in

48 lightweight concrete. In order to simplify the design guidelines for lightweight concrete, the  
49 shear capacity is treated in a similar manner to normal concrete with reduction factors both  
50 with and without a retrofitted system.

51 Externally bonded fibre reinforced polymer (FRP) plates or sheets have proved to be a better  
52 retrofitting system for reinforced concrete (RC) structures compared to traditional  
53 strengthening techniques. FRP has good corrosion resistance, is lightweight and has excellent  
54 mechanical properties. Furthermore, the manual strengthening system allows using the FRP  
55 reinforcements to any member's shape. A significant amount of research has been conducted  
56 to investigate the shear behaviour of normal weight concrete beams strengthened with FRP  
57 composites, including the influence of the strengthening configurations and the bonded length  
58 of the FRP reinforcement (Triantafillou, 1998; Adhikary et al., 2004), shear span to depth  
59 ratio (Khalifa and Nanni, 2002; Lee et al., 2011), size effect (Leung et al., 2007; Foster et al.,  
60 2016), shear reinforcement ratio (Pellegrino and Modena, 2002), the orientation and the  
61 width of the FRP reinforcement (Monti and Liotta, 2007; Sundaraja and Rajamohan, 2009;  
62 Mofidi and Chaallal, 2011), and type of loading (Anil, 2006 and 2008; Carolin and Täljsten,  
63 2005). However, the study of the response of lightweight concrete (LWC) beams  
64 strengthened in shear with reinforcement has not received much attention. Hence, ACI  
65 440.2R (2008) suggests further investigation of the effect of FRP on lightweight concrete.

66 In order to understand the local bond behaviour between the FRP reinforcement and  
67 lightweight concrete, experimental investigation of double-lap shear specimens were  
68 conducted by Al-Allaf et al. (2016). The test results showed that the LWC concrete has a  
69 lower bond strength compared to NWC. It is envisaged that the strengthening of LWC  
70 members will be the significant challenge for structural engineers in the coming decades. In  
71 this paper, therefore, epoxy bonded CFRP strengthening techniques in LWC beams are

72 studied along with NWC in order to verify the shear reduction factors suggested by existing  
73 design guidelines and numerical models, which were developed for NWC.

## 74 **EXPERIMENTAL INVESTIGATION**

75 This study focusses on the behaviour of LWC beams externally strengthened in shear using  
76 carbon fibre reinforced polymers (CFRP) strips. Identical LWC and NWC beams were  
77 prepared and tested under monotonic loading conditions in order to compare the  
78 strengthening techniques and shear resisting mechanisms between LWC and NWC beams.

## 79 **SPECIMEN DESIGN**

80 The entire experimental program comprised six specimens cast with lightweight and normal  
81 weight concretes. Both the NWC and LWC beams were geometrically similar and cast using  
82 the same grade of concrete (i.e. the same compressive strength). The details of each series are  
83 as follows:

- 84 • Series **(BL-UST/CST)** comprised three beams cast with LWC without shear  
85 reinforcement except two shear links adjacent to the supports; one of the beams was  
86 without external CFRP reinforcement and the remaining two beams were each  
87 strengthened with U-shaped (UST) and close (CST) epoxy bonded external CFRP strips.
- 88 • Series **(BN-UST/CST)** comprised three companion beams cast with NWC without shear  
89 reinforcement except two shear links adjacent to supports either side; one beam was used  
90 as a control beam without CFRP reinforcement and two beams were strengthened with  
91 CFRP similar to the LWC beams.

92 All the reinforced LWC and NWC beams were designed to have the same dimensions of 200  
93 mm wide by 300 mm deep and 2000 mm long as shown in Figure 1. The simply supported  
94 beams were loaded under four-point loading conditions with supports located at a distance of

150 mm from the both ends of the beam. Displacement controlled monotonic loading conditions were employed. The shear span to effective depth ratio was taken as  $a/d=2.27$  to secure shear failure which satisfies the definition of a shear beam (Kani, 1966). All the beams were reinforced for flexure with three bottom and two top 16 mm diameter longitudinal deformed steel reinforcing bars (H16 steel bar). The longitudinal steel ratio for both top and bottom reinforcement for all beams was 1.67%. The flexural steel reinforcement was detailed to ensure shear failure of the samples strengthened with CFRP. The effective depth of the beam and the clear cover distance were 264 mm and 28 mm respectively.

### 103 **CONFIGURATION OF CFRP REINFORCEMENT**

104 CFRP reinforcement was used in this test with various shear strengthening systems as  
 105 illustrated in Table 1. Closed-shaped CFRP reinforcements were attached as strips on all the  
 106 faces of the beam. Also, U-shaped systems were attached on the tension (bottom) and the two  
 107 side faces of the beam as strips. The CFRP reinforcements were orientated at  $90^0$  with respect  
 108 to the longitudinal axis of the beam as shown in Figure 2. The width of CFRP reinforcement  
 109 was 100 mm and the spacing of 150 mm from centre-to-centre of the attached CFRP strips.  
 110 These CFRP reinforcements were attached along the shear span of the beam, from the  
 111 support point up to the point of load application on both sides of the beam.

112 Table1: Summary of test parameters

Sample	CFRP ratio (%)	CFRP strengthening type	CFRP orientation	CFRP wrap coverage
BL	0	-	-	-
BL- UST	0.0785	U-shaped	$90^0$	Strip
BL- CST	0.0785	Closed-shaped	$90^0$	Strip
BN	0	-	-	-
BN- UST	0.0785	U-shaped	$90^0$	Strip
BN- CST	0.0785	Closed-shaped	$90^0$	Strip

113

## 114 MATERIAL PROPERTIES

115 Pulverised Fuel Ash (Lyttag) instead of coarse aggregates were used in the preparation of the  
116 lightweight concrete mixture. The particle size grading, physical properties and chemical  
117 composition of the Lytag aggregates are reported by Al-Allaf et al. (2016). The concrete  
118 mixes for both concrete types were designed to have a slump of 75 mm, and a 28-day cube  
119 compressive strength of 40 N/mm<sup>2</sup>. The mix details for the lightweight and normal weight  
120 concretes are given in Table 2. All the LWC and NWC samples were cast in a single batch  
121 each. Furthermore, a total of 18 concrete cubes (100 x 100 x 100 mm), eight concrete  
122 cylinders (150 dia. x 300 mm) and six prisms (100 x 100 x 400 mm) were cast from each  
123 batch to determine the uniaxial compressive strength, the Young's modulus of elasticity, the  
124 concrete density and the modulus of rupture of lightweight and normal weight concretes (see  
125 Table 3).

126 Table 2: The mix design of lightweight and normal weight concretes

Concrete type	Water (kg)	Cement (kg)	Sand (kg)	Coarse aggregate (kg)	Design strength (N/mm <sup>2</sup> )
NWC	192	400	667	1184	40
LWC	216*	480	485	715	40

\* The moisture content and absorption of lightweight aggregates were considered in calculations of mix design.

127

128 Table 3: Mechanical properties of concretes

Concrete type	Average concrete compressive strength (MPa)	Average modulus of rupture (MPa)	Average modulus of elasticity (MPa)	Average concrete density (kg/m <sup>3</sup> )
NWC	42.1	3.49	29860	2356
LWC	43.34	3.026	23510	1823

129

130 For steel reinforcing bars, three samples of longitudinal bars were tested in uniaxial tension.  
 131 Average properties of steel reinforcement are listed in Table 4.

132 Table 4: Mechanical properties of 16 mm diameter steel bar

Yield stress (MPa)	Yield strain ( $\mu\text{m/m}$ )	Ultimate stress (MPa)	Ultimate strain (mm/m)	Modulus of elasticity (GPa)
510	2600	650	130000	200

133  
 134 Mechanical properties of the unidirectional CFRP sheets (C Sheet 240) and primer resin are  
 135 summarised in Table 5 (Weber UK, 2008). Epoxy plus primer (EN-Force primer) and epoxy  
 136 plus adhesive (EN-Force bonding adhesive) were used to bond the CFRP composite to the  
 137 surface of the concrete. Two-thirds of the adhesive as the base component and one-third of  
 138 hardener were used according to the manufacturer's recommendations.

139 Table 5: Mechanical properties of the CFRP sheet and the primer resin (Weber UK, 2008)

<b>CFRP sheet</b>	
Modulus of elasticity	240 GPa
Tensile strength	4000 MPa
Strain at failure	1.6%
<b>Primer resin</b>	
Compressive strength	100 N/mm <sup>2</sup>
Tensile strength	19 N/mm <sup>2</sup>
Flexural strength	30 N/mm <sup>2</sup>
Bond to concrete	> 5.3 N/mm <sup>2</sup>
Modulus of elasticity	5 kN/mm <sup>2</sup>

141  
 142 A concrete grinder machine was used to smooth the surface of the concrete in order to  
 143 achieve the required level of stress transference between the CFRP and the surface of the  
 144 concrete. Then, the surface was cleaned to remove the dust produced during the grinding  
 145 process. Samples corners were rounded to prevent unwanted CFRP rupture which can be  
 146 developed as a result of the high-stress concentration in the CFRP reinforcement wrapped



147 close the corner of the beam. For the U-shaped systems, the CFRP reinforcement was  
148 attached directly below the top surface of the beams by approximately 20 mm.

149

## 150 **TEST ARRANGEMENT**

151 The four-point loading arrangement shown in Figure 3 was used. A 500 kN load cell attached  
152 to a hydraulic jack was used to record the applied load during the test, with monotonic loads  
153 applied via a spreader beam. This spreader beam was seated on 25 mm diameter steel rollers  
154 welded to steel plates (length=200 mm and width=100 mm) bedded on the top surface of the  
155 sample to avoid local crushing of concrete at the load point. The sample is placed over the  
156 two support points with a 25 mm diameter steel roller seated on the top surface of a 100 mm  
157 steel plate. One of the steel rollers was welded to the steel plate, and a (length=200 mm and  
158 width=100 mm) steel plate was provided on top of the roller to avoid local crushing of  
159 concrete at the support as shown in Figure 3.

## 160 **INSTRUMENTATION**

### 161 **Steel Strain Gauges**

162 Ten FLA-6-11 uni-directional strain gauges by Tokyo Sokki Company were used to record  
163 the strain measurements at different positions along the length of the middle bar in the bottom  
164 layer in each of the normal and lightweight samples. The gauge factor, gauge resistance and  
165 the gauge length were  $2.12 \pm 1$  %,  $120 \pm 0.5$   $\Omega$  and 6 mm respectively. Strain gauges were  
166 positioned externally at 250 mm, 400 mm, 550 mm, 700 mm, and 850 mm from both ends of  
167 each beam, as shown in Figure 4. The gauges were denoted as “LS” combined with a number  
168 starting from 1 to 10 to identify their location from the left end of the beam.

169 **CFRP Strain Gauges**

170 Figure 5 illustrates the strain gauges employed in the CFRP reinforcement during the test.  
171 The strain gauges and CFRP strip were denoted as “SG” and “SF” respectively. The type  
172 FLA-5-11 strain gauge by Tokyo Sokki Company measures a uni-directional strain, which  
173 was orientated vertically and has a gauge factor and length of 2.12% and 5 mm respectively.  
174 The same arrangements were employed for all LWC and NWC strengthened samples.

175 **Linear Variable Differential Transformers (LVDTs)**

176 Three Linear Voltage Displacement Transducers (LVDTs) were used in this test to record  
177 vertical deflections at various positions along the sample as shown in Figure 6. The LVDTs  
178 were mounted on a frame connected to the centre of concrete directly above the supports to  
179 measure the relative displacement along the beams.

180 **EXPERIMENTAL RESULTS**

181 A summary of the samples shear strength based on the maximum shear carrying capacity, the  
182 recorded mid-span deflection and the modes of failure are summarised in Table 8.

183 Table 8: Summary of the shear capacities, failure deflection and modes of failure

Sample	Max Shear capacity (kN)	Mid-span Deflection at failure (mm)	Failure mode, CFRP failure
BL	151.78	4.82	Failure in shear
BL-UST	218.38	7.10	Failure in shear due to CFRP debonding
BL-CST	267.14	11.3	Failure in shear due to CFRP rupture
BN	164.1	5.35	Failure in shear
BN-UST	248.6	7.69	Failure in shear due to CFRP debonding
BN-CST	320.8	10.3	Failure in shear due to CFRP rupture

184  
185 Comparison of the maximum shear failure loads between CFRP-retrofitted samples and the  
186 reference sample reveals that the CFRP retrofitting systems were efficient in improving the

187 shear strength of the LWC and NWC beams. Figure 7(a) shows the shear strength gained due  
188 to CFRP reinforcement in the strengthened samples compared with the corresponding control  
189 samples of LWC and NWC. For the LWC series, the shear strength provided by CFRP  
190 reinforcement for U-shaped and Closed-shaped samples were 44% and 76% respectively,  
191 when compared with the control sample, while for the NWC series, the shear strength  
192 provided by CFRP reinforcement for U-shaped and Closed-shaped samples were 51% and  
193 95% respectively.

194 In this study, the shear strength of the control, U- shaped and Closed-shaped samples of LWC  
195 are 92%, 87% and 83% of the control, U-shaped and Closed-shaped samples of the  
196 corresponding NWC samples respectively.

197 All the strengthened samples demonstrate increases in the maximum deflection over the  
198 control samples at failure as shown in Figure 7(b) and Table 8. LWC and NWC samples  
199 strengthened with U- shaped CFRP had 47% and 43% greater maximum deflection at failure  
200 over the control LWC and NWC samples. Comparison with samples strengthened with  
201 Closed-shaped CFRP had an increase in maximum deflection at failure of 134% and 93%  
202 respectively. This observation resulted from the evidence that crack bridging forces provided  
203 by CFRP reinforcements could increase the shear strength of LWC and NWC beams and  
204 yielded a better ductility over the control samples. In contrast, LWC samples demonstrated  
205 lower shear enhancement while producing higher ductile behaviour compared to  
206 corresponding NWC samples. Increases in interfacial and shear stresses with increasing  
207 plastic deformation leads to CFRP debonding and unexpected CFRP rupture failures, thus the  
208 effectiveness of FRP for shear strengthening LWC beams will be affected by this issue. This  
209 observation can be attributed to a lower concrete surface tensile strength, aggregate interlock  
210 at the diagonal crack faces and requirement for longer effective bond length in LWC as  
211 observed by Al-Allaf et al. (2016 and 2015). CFRP bond deterioration in LWC requires

212 consideration to ensure the safety of CFRP applications for shear strengthening of LWC  
213 beams.

## 214 **LOAD-DEFLECTION RESPONSE**

215 The shear-deflection response curves for all the specimens are compared in Figure 8. The  
216 behaviour trends for NWC and LWC samples are described by three zones of stiffness's: (i)  
217 elastic stiffness zone (elastic behaviour), (ii) flexural stiffness zone, and (iii) shear stiffness  
218 zone. In general, all LWC and NWC beams showed the same elastic stiffness zone before  
219 first flexural cracks (approximately 50 kN). The flexural stiffness zone showed the same  
220 linear trend until a diagonal crack appeared at the surface of concrete at the applied load  
221 between 100-130 kN load range for NWC beams and 90-120 kN load range for LWC beams.

222 As illustrated in Figure 8, the lightweight control sample (BL) reached a maximum load of  
223 151.78 kN and corresponding mid-span deflection of 4.30 mm. An abrupt increase in applied  
224 load developed at this stage as a result of the diagonal shear crack opening width. The  
225 strengthened LWC samples (BL-UST and BL-CST) exhibit identical stiffness at low level  
226 loading. This can be attributed to the configuration of the CFRP which would not influence  
227 the stiffness until the diagonal shear crack developed. However, at the maximum load for  
228 Closed-shaped samples, the shear cracking zone was considerably higher than those observed  
229 in the samples with the U-shaped system. This is assigned to the premature failure for  
230 samples strengthened with the U-shaped system where effective length of CFRP bond was  
231 not available. It can be noticed that the NWC samples displayed similar shear deflection  
232 shapes to the corresponding LWC samples.

233 Figure 8 also shows that the stiffness of LWC samples is lower than those of NWC samples  
234 with identical CFRP strengthening configurations after initial cracking. This behaviour is a  
235 result of the variance in rigidities of the LWC tested samples. LWC samples had lower

236 stiffness compared with NWC samples due to lower stiffness of lightweight aggregate  
 237 (LWA) particles and higher cement ratio (Clarke, 2002).  
 238 Both controlled and U-shaped LWC and NWC samples (BL, BN, BL-UST and BN-UST)  
 239 failed immediately after reaching the maximum load carrying capacity. This is due to the fact  
 240 that the crack bridging force across the diagonal crack was not available or fully reached its  
 241 capacity in the controlled and U-shaped retrofitted systems respectively. However, both  
 242 closed-shaped LWC and NWC samples (BL-CST and BN-CST) exhibited a plastic behaviour  
 243 before the rupture of CFRP sheets.

## 244 FAILURE MODES

245 All the tested LWC and NWC beams failed in shear by initiation of diagonal tension cracks  
 246 in the shear span. Loss of friction at the crack interfaces and shear rotation were the failure  
 247 modes of the control samples. In the case of samples retrofitted with CFRP reinforcements,  
 248 the CFRP strips either debonded or ruptured as shown in Figure 9. The inclinations of  
 249 diagonal tension shear cracks are summarised in Table 9, which are numbered from 1 to 3  
 250 according to their location from the left end of the beam. In general, the orientation of the  
 251 diagonal tension crack for strengthened samples was lower than their corresponding control  
 252 samples. Furthermore, there is no variance in response between corresponding lightweight  
 253 and normal weight samples regarding the inclinations of diagonal shear cracks despite the  
 254 clear difference in ultimate shear loads.

255 Table 9: Inclination of diagonal shear cracks

Sample	Inclination of diagonal shear cracks			Average inclination
	$\theta_1$	$\theta_2$	$\theta_3$	
BL	42 <sup>0</sup>	40 <sup>0</sup>		41 <sup>0</sup>
BL-UST	34 <sup>0</sup>	30 <sup>0</sup>		32 <sup>0</sup>
BL-CST	33 <sup>0</sup>	37 <sup>0</sup>	35 <sup>0</sup>	35 <sup>0</sup>
BN	41 <sup>0</sup>	44 <sup>0</sup>		42 <sup>0</sup>
BN-UST	33 <sup>0</sup>			33 <sup>0</sup>
BN-CST	35 <sup>0</sup>	37 <sup>0</sup>	34 <sup>0</sup>	35 <sup>0</sup>

256

257 The CFRP reinforcements have significant effects on the beams crack distributions. The  
258 CFRP reinforcements delay the loss of friction by reducing the diagonal crack opening width.  
259 This was achieved by the confinement and crack bridging effects of CFRP. At the ultimate  
260 limit state, the crack bridging effect was lost and the loss of friction occurred suddenly  
261 without any warning. The failure patterns are extremely brittle when compared to the control  
262 samples. The same failure modes were observed by Bousselham & Chaallal (2008).

263 Shear failure as a result of CFRP debonding was the failure mode of the LWC sample  
264 strengthened with U-shaped CFRP (BL-UST). The failure in bond between CFRP and  
265 concrete was initiated by debonding in a thick layer of lightweight concrete close the surface  
266 of the beam, (see Figure 9(c)). The CFRP reinforcement was detached locally from the  
267 surface of concrete at the diagonal shear cracks. With more loading, the debonding failure  
268 gradually extended from the crack and moved away towards the top and the bottom of the  
269 beam. A similar failure mode was observed for the NWC sample strengthened with U-shaped  
270 CFRP (BN-UST) except the CFRP debonding initiated with a thin layer of normal concrete  
271 (close to the concrete surface)(see Figure 9(d)). Generally, BL-UST showed higher crack  
272 intensity and widths compared with BN-UST. The average major diagonal crack widths in  
273 BL-UST and BN-UST were about 7 and 4 mm respectively.

274

275 In contrast, LWC and NWC samples strengthened with Closed-shaped CFRP (BL-CST and  
276 BN-CST) failed due to CFRP rupture (see Figure 9(e) and (f)). CFRP fibres across the  
277 diagonal shear crack snapped one-by-one because of excessive straining. These samples also  
278 failed in extremely brittle manner compared with the control samples. Furthermore, CFRP  
279 rupture caused larger increases in shear strength compared to CFRP debonding failure. This  
280 can be attributed to longer effective bond length in the Closed-shaped CFRP. Each of the

281 samples had few diagonal shear cracks. However, no significant difference in the crack  
282 pattern was observed between lightweight and normal weight samples. Furthermore, the  
283 failures of the samples were due to a single diagonal crack. The average major diagonal crack  
284 widths in BL-CST and BN-CST were about 4 and 3 mm respectively.

285 It was noticed that the LWC samples exhibited low shear strengths and weaker friction  
286 between crack faces. In this study, microstructural examinations using a light microscope and  
287 a scanning electron microscope (SEM) were conducted on a sample of lightweight and  
288 normal weight concrete collected from the crack faces in order to examine the macro/micro  
289 and nano internal pore structures. These methods were implemented to support the behaviour  
290 observed in the disruptive failure test. Interestingly, light micrographs of lightweight concrete  
291 samples show that the path of diagonal tension cracks propagated through the lightweight  
292 aggregates (see Figure 10 (a)) rather than in the concrete matrix around the aggregates as in  
293 normal weight samples (see Figure 11 (a)). This could be attributed to the lower tensile  
294 strength of lightweight aggregate compare to normal weight aggregate. Hence, it can be  
295 concluded that the energy required for the crack opening through the lightweight aggregates  
296 is less than the crack propagation around the coarse aggregates. Due to the cracks though the  
297 aggregates, the crack faces do not have a significant amount to surface interlock, which is  
298 common in normal weight concrete. Therefore, the aggregate interlock between the crack  
299 faces could be neglected in lightweight concrete beams and this eventually leads to the lower  
300 shear capacity of lightweight concrete beams.

301 The SEM micrographs of the lightweight concrete sample revealed the spherical shapes of  
302 Lytag particles with an extremely porous microstructure (see Figure 10 (b) to (e)). In contrast,  
303 the normal weight aggregates are angular in shape with a non-porous surface (see Figure 11  
304 (c)). Furthermore, the lightweight aggregate is surrounded by an orange coloured area  
305 (reacted zone) (see Figure 10 (a)). This is due to the chemical reaction between the

306 lightweight particles and the cement matrix. Figure 10 (c) shows the reacted zone and the  
307 microstructure of lightweight particles, in which the voids are considerably higher than the  
308 cement paste. Also, Figure 10 (d) illustrates the boundary between the reacted zone and the  
309 cement paste. It can also be observed that the cement paste and lightweight particles are well  
310 interlocked as illustrated in the typical microstructure of the interfacial zone for a composite  
311 of Lytag particle and cement paste (see Figure 10 (a)).

312 Figures 11(b) and (d) show that the normal aggregates are bonded with the cement paste  
313 rigidly and cracks develop around the aggregates. In this case the aggregate interlock between  
314 the crack faces potentially provides significant contribution to the ultimate shear carrying  
315 capacity.

## 316 **LONGITUDINAL STEEL STRAIN**

317 The longitudinal steel reinforcement was slightly strained at the earlier stage of loading and  
318 starts to elongate with the occurrence of flexural or shear cracks. Yielding of the central steel  
319 bar was not observed in the control normal and lightweight samples due to premature shear  
320 failure. Furthermore, it was noted that the tested samples showed approximately the same  
321 elongations at a low level of loading on both sides of the LWC and NWC samples.  
322 Longitudinal steel strain profiles of samples BL-CST and BN-CST at various load levels  
323 (20%, 40%, 60%, 80%, and 100% of the maximum shear capacity) are presented in Figure  
324 12, where the horizontal black line represents the yield strain of the steel. Variance in strain  
325 measurements was noticed at a higher level of loading in several samples, which can be  
326 attributed to the position, number and effect of diagonal shear and flexural cracks. For BL-  
327 CST, the recorded strains close to the centre of the beam are lower compared with  
328 corresponding BN-CST, except at the ultimate load (100%) as shown in Figure 12 (a) and  
329 (b). Similar behaviour was observed between the BL-UST and BN-UST samples. This  
330 behaviour can be attributed to the multiple hair-line flexural cracks observed in the middle of



331 the beam and initiation of shear cracks close to the applied load for the normal weight  
332 concrete samples. In contrast, diagonal shear cracks close to support in lightweight concrete  
333 samples were prevalent. The strain distributions at the ultimate load of both LWC and NWC  
334 samples were similar. Hence, the contribution of dowel action by longitudinal reinforcement  
335 for shear resistance in LWC and NWC samples could be considered as the same at the  
336 ultimate load (Martin-Perez and Pantazopoulou, 2001).

### 337 **CFRP STRAIN**

338 The average strain response of CFRP reinforcement is characterised by two stages: the first  
339 stage is where the CFRP strains are very small and the second stage where an abrupt increase  
340 of CFRP strains develops with further loading. The first considerable increase in CFRP  
341 strains developed at an applied load of 100 kN for BL-UST, 120 kN for BL-CST, 110 kN for  
342 BN-UST and 130 kN for BN-CST. It can be noted that the LWC samples has a slightly lower  
343 applied load at the point of shear crack initiation. This observation was related to the crack  
344 propagation across the CFRP strips. This crack would subsequently initiate into the diagonal  
345 shear crack that could lead to failure of the sample. Up to this loading point (initial crack  
346 load), the contribution of the CFRP reinforcement to the total shear strength of the reinforced  
347 concrete beam is very small and can be ignored. With further loading, the crack opening  
348 increases and new shear cracks develop, leading to an increase in CFRP stress due to crack  
349 bridging forces of the CFRP strips. The sudden decrease in CFRP strains which is observed at  
350 higher level of loading in some of the instrumented CFRP strips for samples with U-shaped  
351 reinforcement. This is could be attributed to the global debonding of the CFRP reinforcement  
352 from the surface of the concrete.

353 The CFRP strains of all the effective straps at the failure loads are summarised in Table 10. A  
354 significant difference in measured CFRP strains between U-shaped and Closed-shaped  
355 samples were observed. This is attributed to the premature failure of samples with the U-

356 shaped strengthening technique. Samples with Closed-shaped CFRP reinforcement were able  
357 to sustain larger strains compared with U-shaped samples.

358 Generally, the stress distribution in the RC beam is complex and may affect the CFRP-to-  
359 concrete interface, with an expectation to accelerate CFRP debonding and to minimise the  
360 maximum debonding strain. The increase in interfacial and normal stresses with increasing  
361 plastic deformation in lightweight concrete beams leads to unexpected CFRP reinforcement  
362 failures and thus a reduction in the maximum debonding strains.

363 Table 10: Summary of maximum local CFRP strains at sample failure

Sample	Shear force (kN)	Strains at failure from individual gauges at each instrumented CFRP strips ( $\mu\text{m/m}$ )					
		SF1	SF2	SF3	SF4	SF5	SF6
BL-UST	218.4	4011.6	4725.9	2911.0	<b>4728.6</b>	4216.7	1662.4
BL-CST	267.1	5819.4	<b>5972.5</b>	4800.3	2788.3	4466.5	1846.8
BN-UST	248.6	2120.8	<b>5837.5</b>	664.5	1642.6	846.1	4919.4
BN-CST	320.8	2393.0	<b>9416.0</b>	7893.2	2579.8	1948.1	4711.9

## 364 NUMERICAL ANALYSIS

### 365 SHEAR COMPONENT ANALYSIS

366 The shear contribution of CFRP was calculated using two different methods. Firstly the  
367 subtraction method allows the calculation of the shear contribution provided by the concrete  
368 and CFRP reinforcements using the difference in failure loads between samples, which is  
369 useful in understanding the efficiency of CFRP reinforcement. This method is derived based  
370 on the concept that the shear contribution by the additional confinement effect of concrete in  
371 the presence of CFRP at failure load could be negligible (Khalifa and Nanni, 2002). This  
372 method can be illustrated using a simple free-body diagram of half of the cracked beam as  
373 shown in Figure 13.

374 Secondly, the shear contribution of the CFRP strips can be evaluated by summing the  
375 contribution provided by CFRP reinforcement across the diagonal shear crack at each side of  
376 the beam, as shown in Equation 1:

$$V_f = \sum_{i=1}^n A_{fi} E_f \varepsilon_{fi} \quad (1)$$

377 where  $V_f$  is the estimated shear force provided by the CFRP reinforcement,  $A_f$  is the area of  
378 the CFRP strip,  $E_f$  is the elastic modulus of CFRP material,  $\varepsilon_f$  is the strain determined from  
379 strain gauges attached to the CFRP strip and  $n$  is the number of stirrups or CFRP strips  
380 crossing the observed critical shear crack,. The relative contribution of shear resistance by  
381 various mechanisms (i.e., tensile strength of concrete, aggregate interlock at the diagonal  
382 crack faces, compressive strength of concrete, interfacial shear stress, dowel action provided  
383 by the longitudinal steel reinforcement) were not fully understood so far (Kim, 2011). Hence,  
384 the shear contributions of these mechanisms of concrete beam with longitudinal  
385 reinforcement were considered together in this study. The concrete contribution ( $V_c$ ) was  
386

387 obtained by subtracting the estimated contributions of CFRP reinforcement ( $V_f$ ) from the  
388 total shear capacity at a particular load level ( $V_t$ ) as given by Equation (2):

$$V_c = V_t - V_f \quad (2)$$

389  
390 Figure 14 shows the results of the shear component analysis for the LWC and NWC beam  
391 specimens. In these figures, the horizontal axis represents the total applied load recorded by  
392 the load cell and the vertical axis represents the total shear contribution of concrete and CFRP  
393 reinforcements on both sides of the beam. It can be noted that the shear strength provided by  
394 CFRP reinforcement was very small and can be ignored before the occurrence of a diagonal  
395 shear crack. In this stage, external loads applied to the samples are mainly resisted by the  
396 concrete. As the diagonal shear crack develops, a part of the load is taken by the CFRP  
397 reinforcement as demonstrated by a sudden leap in the CFRP shear contribution response  
398 curves. The CFRP reinforcement gradually carries the external shear force until the CFRP  
399 reinforcement detaches from the surface of the concrete or ruptured. Abrupt falls in the CFRP  
400 shear contribution can be highlighted when the CFRP reinforcement debonds or ruptures  
401 before the sample failure (see Figure 14(c)). A similar response was observed in experimental  
402 investigations conducted by Bousselham and Chaallal (2008). It can be concluded that there  
403 was virtually no difference between the lightweight samples and their normal weight  
404 companions regarding the general trend of the CFRP reinforcement contribution, a similar  
405 response was observed for all the tested samples. However, the contribution of CFRP in  
406 LWC is slightly lower than the corresponding NWC samples.

407 Table 11 summarises the maximum shear contribution provided by concrete and the CFRP.  
408 Interestingly, the CFRP contribution to shear using the subtraction method of analysis is very  
409 close to the values when the strain readings are used to evaluate the shear strength component  
410 provided by CFRP reinforcement. Hence the additional confinement effect in the presence of  
411 CFRP can be neglected based on the subtraction method of analysis.

412

413 Table 11: Maximum shear contribution provided by concrete and the CFRP reinforcement

Sample	Total shear capacity (kN)	Subtraction Method of Analysis (kN)	Shear strength provided by concrete and CFRP reinforcement	
			$V_f$ (kN)	$V_c$ (kN)
BL	151.78	0	0	151.78
BL-UST	218.38	66.6	68.6	149.82
BL-CST	267.14	115.4	118.6	148.53
BN	164.1	0	0	164.1
BN-UST	248.6	84.5	84.1	164.3
BN-CST	320.8	156.7	159.7	161.1

414

415 **COMPARISON WITH DESIGN CODES AND GUIDELINES**

416 Current design codes and guidelines such as ACI 318-08 (2008), CAN/CSA-S6 (2006) and  
417 Eurocode2 (2014) present calculations for the shear carrying capacity of normal weight  
418 reinforced concrete beams. In order to calculate the shear resistance of lightweight concrete,  
419 a reduction factor was proposed. ACI 318-08 suggests to use 0.85 as the reduction factor.  
420 Eurocode 2 provides a reduction factor which is related to density of the lightweight concrete.  
421 However, the shear prediction of CAN/CSA-S6 includes the density of concrete. Therefore,  
422 the density of lightweight concrete could be used for the prediction of shear strength. Shear  
423 predictions of normal and lightweight concretes illustrates that the CAN/CSA-S6 are close to  
424 experimental results (see Table 12). The predication of ACI 318-08 and Eurocode 2  
425 underestimate the shear capacity of the control lightweight and normal weight samples. This  
426 may be attributed to the arching effects developed by the low shear span-to-depth ratio  
427 ( $a/d=2.2$ ) which increases the shear resistances of the tested samples.

428 Table 12: Experimental and predicted results of control samples

Sample	Experimental result (kN)	ACI 318-08 (kN)	Eurocode 2 (kN)	CAN/CSA-S6 (kN)
BN	164.1	116.6	120.3	164.6
BL	151.8	100.5	100.3	137.9

429

430 Furthermore, ACI 440.2R (2008), TR-55 (2013) and CAN/CSA-S6 (2006) allow the  
 431 estimation of the contribution of CFRP separately to the concrete contribution. The  
 432 experimental results (using the subtraction method of analysis, from Table 11) and numerical  
 433 predictions using the current design codes for the CFRP contribution of the tested LWC and  
 434 NWC beams are summarised in Table 13.

435 Table 12: Experimental and predicted results of CFRP shear contribution for strengthened  
 436 samples  
 437

Sample	CFRP contribution from subtraction method (kN)	ACI 440.2R (kN)	TR-55 (kN)	CAN/CSA-S6 (kN)
BL-UST	66.6	73.6	72.1	71.6
BL-CST	115.4	79.6	79.6	79.6
BN-UST	84.5	73.4	70.2	71.6
BN-CST	156.7	79.6	79.6	79.6

438  
 439 The predictions of the ACI 440.2R (2008), TR-55 (2013) and CAN/CSA-S6 (2006)  
 440 overestimate the contributions of U-shaped CFRP reinforcement of the LWC retrofitted beam  
 441 (BL-UST). These codes use the concrete compressive strength for the prediction of CFRP  
 442 contribution. As noticed, the tensile strength and the bond strength between lightweight  
 443 concrete and FRP are significantly low compared to normal weight concrete while  
 444 compressive strengths are the same. Furthermore, BL-UST has a limited bond length.  
 445 Therefore, the prediction of the CFRP contribution on LWC beams using design guidelines  
 446 should be modified with available effective length and tensile strength of concrete.

447 **CONCLUSION**

448 This study investigated the efficiency of epoxy-bonded CFRP strips on lightweight concrete  
449 in shear. While the normal weight concrete samples agrees with the existing experimental and  
450 numerical studies, the following conclusion can be derived on lightweight concrete samples:

- 451 • The shear strength gained due to CFRP reinforcement for lightweight samples is less  
452 than the normal weight concrete samples. This is probably attributed to lower concrete  
453 surface tensile strength and aggregates interlock.
- 454 • The test observations reveal that there was virtually no difference between the  
455 lightweight beams and their normal weight companions regarding the failure modes and  
456 shear cracks inclinations. However, it was noticed that the path of diagonal tension  
457 cracks on the tested LWC samples propagated through coarse aggregates rather than in  
458 the concrete matrix around the aggregates as in normal weight samples. It can be also  
459 concluded that the LWC samples had higher cracks width due to lower aggregate  
460 interlock at the primary shear crack interface.
- 461 • Samples with Closed-shaped CFRP reinforcement experienced higher CFRP strains  
462 compared with U-shaped sample, which failed due to the premature debonding of the  
463 CFRP reinforcement from the surface of concrete. Furthermore, numerical predictions  
464 using design guidelines and codes overestimate the CFRP contribution in the  
465 lightweight concrete beam strengthened with U-shaped CFRP system. This is result of  
466 insufficient bond length, which significantly influenced by the tensile strength of  
467 lightweight concrete (Al-Allaf et al., 2016).
- 468 • Therefore, the effect of CFRP on lightweight concrete should receive more attention in  
469 the current design codes and guidelines, which were derived and verified using  
470 experimental results of FRP strengthened system on normal weight concrete. Further

471 analytical and experimental studies are required to include the characteristics of the  
472 FRP/ lightweight joints in current codes and guidelines to evaluate the efficiency of  
473 using FRP reinforcement to strength LWC structures where the effective bond could not  
474 be achieved.

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