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# On the Performance of DF-based Power-Line/Visible-Light Communication Systems

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**Abstract**—This paper presents a comprehensive performance analysis of an integrated indoor power line communication (PLC)/visible light communication (VLC) system with the presence of a decode-and-forward (DF) relay. The existing indoor power line networks are used as the backbone for VLCs. The performance of the proposed system is evaluated in terms of the average capacity and the outage probability. A new unified mathematical method is developed for the PLC/VLC system and analytical expressions for the aforementioned performance metrics are derived. Monte Carlo simulations are provided throughout the paper to verify the correctness of the analysis. The results reveal that the performance of the proposed system deteriorates with increasing the end-to-end distance and improves with increasing the relay transmit power. It is also shown that the outage probability of the system under consideration is negatively affected by the vertical distance to user plane.

**Index Terms**—Decode-and-forward (DF), power line communications (PLC), signal-to-noise ratio (SNR), visible light communications (VLC).

## I. INTRODUCTION AND RELATED WORKS

**R**ELIABLE communications can be achieved by integrating different networks such as power line communication (PLC) with visible light communication (VLC) and PLC with wireless communication systems. Such systems have been studied by many researchers and have shown very promising solutions in terms of capacity, security and data rate improvements [1], [2]. Exploiting the existing power line networks in buildings and utility grids makes such networks one of the competitive technologies for broad-band communications in indoor applications. The other technology, which is expected to play an essential role in such applications, is the optical wireless communication (OWC). VLC is one of the indoor OWC technologies which has attracted a considerable attention because of the widespread usage of the LEDs.

Recently, the adoption of other communication technologies for PLC and VLC systems has motivated many researchers to implement different relaying protocols to further enhance the system performance, the most common of which are decode-and-forward (DF), amplify-and-forward (AF), incremental DF and selective DF relaying, see e.g., [3]–[8].

The implementation of half duplex time division relaying protocols with indoor PLC applications has been investigated by the authors in [4]. The authors in [9] concluded that the relay deployment in wireless systems is by far more efficient than that in PLC systems. Two-way relaying and one-way relaying were discussed in [3] where the authors reported

that there is a significant improvement in system performance by utilizing the former compared to the latter. The authors in [10] investigated the deployment of multi-way relaying in parallel for indoor PLC applications. It was found that the achievable data rates were relatively high compared to those accomplished by single transmission. The study in [1] discussed the hybrid PLC/wireless system performance in the presence of AF relaying where the source of the information simultaneously transmits data via both networks PLC and wireless. It was reported that the integrated PLC/wireless system outperforms the PLC-only and the wireless-only systems. The performance of cooperative free space optics (FSO)-VLC communication system in terms of capacity with a DF relay was investigated in [5]. The FSO link was the backbone of the VLC system and the DF relay was located in-between the two links. It was concluded that this system has high efficiency in terms of data rate. The cooperation between light sources and how it can improve the performance of VLC systems was investigated in [11] where the authors reported that the implementation of DF relaying offers better performance than that of AF relaying.

To the best of the authors knowledge, only few works have studied the performance of cascaded PLC/VLC links in the presence of DF relaying protocols in terms of capacity and outage probability. Therefore, this paper investigates the implementation of DF relaying to connect PLC and VLC links via a DF relay. In the proposed system, the information source first sends the information signal to a DF relay through a PLC link. Secondly, the DF relay decodes and forwards the received signal to the destination node via the VLC channel. The major contribution of this work resides in deriving analytical expressions for the average capacity and the outage probability of the proposed hybrid PLC-VLC DF-based system. Formulating the overall capacity and outage probability of the proposed PLC/VLC system offers the opportunity to examine the effect of various system parameters on the communication performance.

The rest of the paper is organized as follows. The system model is described in Section II. Section III presents the system performance analysis. Discussions of the numerical results are presented in Section IV. Finally, the conclusions of this paper are drawn in Section V.

## II. SYSTEM MODEL

The system model under consideration is shown in Fig. 1 where PLC users can be connected to the network through PLC modems. We assume that the source node and the VLC

user are in a different floors. The DF relay receives the data from the source node via the PLC link. The data is then decoded and re-transmitted by the DF relay to the end user through the VLC link. The complex channel gains  $h_P$  and  $h_v$  represent the source-to-relay, (i.e., the PLC link) and the relay-to-destination, (i.e., the VLC link) channel gains, respectively. Both channels are assumed to be independent and identically distributed. The channel distribution of the PLC link is log-normal distribution [12]. In this study, we consider the line-of-sight (LOS) component of the down-link transmission of the LED only as it represents more than 90% of the total received signal [13]. The LED is located on the ceiling with a vertical distance to the user plane  $L$  and Euclidean distance to the destination  $d_k$ . The VLC channel is subjected to a random distribution which is affected by the uniform distribution of the user's location [13]. Because of the nature of the network structure adopted here, it is logical to assume that there is no direct link between the source and destination nodes. It is worth mentioning, for simplicity and without loss of generality, that noise over the two links is assumed to be additive white Gaussian noise (AWGN).

### III. PERFORMANCE ANALYSIS

#### A. Average Capacity

The instantaneous capacity of the hybrid system is given by the following

$$C = \min(C_{PLC}, C_{VLC}), \quad (1)$$

where  $C_{PLC}$  and  $C_{VLC}$  are the instantaneous capacities of the PLC and VLC links, respectively.

Therefore, each link capacity should be derived in order to find the overall capacity. We start with the PLC link which connects the transmitter with the DF relay and acts as a backhaul to the VLC link. The signal at the relay can be given by

$$y_r(t) = \sqrt{P_s} e^{-\alpha d} h_{PLC} s(t) + n_r, \quad (2)$$

where  $P_s$  represents the source transmit power,  $d_1$  represents the source-to-relay distance,  $s(t)$  is the information signal with  $E[s]=1$ ,  $n_r$  is the noise at the relay which is assumed to be complex Gaussian with zero mean and variance  $\sigma_r^2$ , and  $\alpha$  is the PLC channel attenuation factor given by  $\alpha = a_0 + a_1 f^k$ , where  $a_0$  and  $a_1$  are constants determined by measurements,  $f$  is the system operating frequency and  $k$  denotes the exponent of the attenuation factor [14].

The signal-to-noise ratio (SNR) at the DF relay can be written as follows

$$\gamma_r = \frac{P_s e^{-2\alpha d} |h_{PLC}|^2}{\sigma_r^2}. \quad (3)$$

Mathematically, we can calculate the average capacity of the PLC link as [14]

$$\mathbb{E}[C_{PLC}] = \sum_{n=1}^{N_p} \frac{1}{\sqrt{\pi}} H_{x_n} h(x_n), \quad (4)$$

where  $H_{x_n}$  represents the weight factors of the  $N_p$  order Hermite polynomial,  $x_n$  is the zeros of the same order and

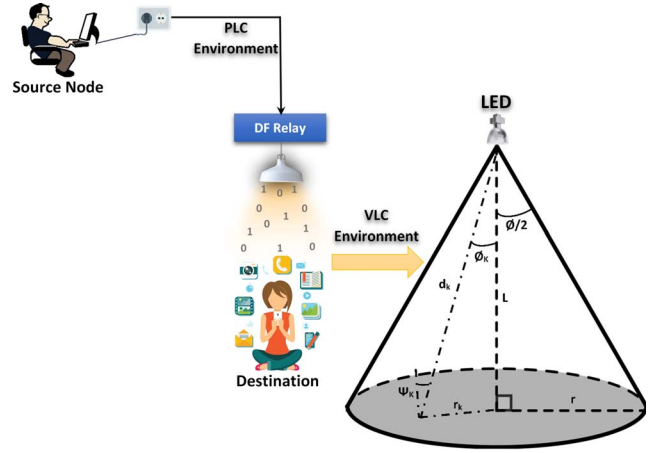


Fig. 1: System model for the hybrid PLC/VLC network for indoor communication applications.

$$h(x_n) = \log_2 \left( 1 + \exp \left( \frac{\sqrt{8}\sigma x_n + 2\mu + \zeta \ln(a)}{\zeta} \right) \right), \quad (5)$$

where  $\zeta$  is the scaling constant and is equal to  $10/\ln(10)$ ,  $\mu$  and  $\sigma$  are the log-normal parameters, and  $a = \frac{P_s e^{-2\alpha d}}{\sigma_d^2}$ . Now we calculate the average capacity of the VLC link. The received signal at the VLC user can be expressed as

$$y_d(t) = s_2(t) h_v \sqrt{P_r} + n_d, \quad (6)$$

where  $s_2(t)$  is the information signal with  $E[s]=1$ ,  $P_r$  is the relay transmit power and  $n_d$  represents the destination noise with zero mean and variance  $\sigma_d^2$ .

The SNR at the destination can be written as

$$\gamma_d = \frac{G^2 P_r |h_v|^2}{\sigma_d^2}. \quad (7)$$

The average capacity of the VLC link is calculated as

$$\mathbb{E}[C_{VLC}] = \int_{t_{min}}^{t_{max}} \log_2(1 + \gamma) f(\gamma) d\gamma, \quad (8)$$

where  $f(\gamma)$  is the probability density function (PDF),  $t_{min} = \frac{(Q(m_k+1)L^{m_k+1})^2}{(r^2+L^2)^{m_k+3}}$  and  $t_{max} = \frac{(Q(m_k+1)L^{m_k+1})^2}{L^{2(m_k+3)}}$ .

Considering the random distribution mentioned above for the VLC link and the Lambertian radiation pattern for LED light emission, the VLC channel gain  $h_v$  can be written as

$$h_v = \frac{m_k + 1}{2\pi d_k^2} A_d \cos^{m_k}(\phi) \cos(\Psi_K) U(\Psi_K) g(\Psi_K) R_p, \quad (9)$$

where  $A_d$  is the detection area of the detector,  $d_k = \sqrt{r_k^2 + L^2}$ ,  $U(\Psi_K)$  represents the optical filter gain,  $g(\Psi_K)$  denotes the optical concentration gain, the responsivity of the photo-detector is represented by  $R_p$ ,  $\phi$  is the total angle of the LED,  $\cos^{m_k}(\phi) = \cos(\Psi_K) = \frac{L}{\sqrt{r_k^2 + L^2}}$ , and

$$\mathbb{E}[C_{VLC}] = \frac{1}{2\log[2]} \int_{t_{min}}^{t_{max}} \log \left[ 1 + \frac{P_r}{\sigma_d^2} h \right] \left( \frac{-Q^{\frac{2}{2+m}} ((m_k + 1) L^{m_k+1})^{\frac{2}{m+3}} h^{-\frac{m_k+4}{m_k+3}} h^{\frac{1}{m_k+3}}}{(m_k + 3)r^2} \right). \quad (16)$$

$$\begin{aligned} \mathbb{E}[C_{VLC}] &= \frac{\frac{1}{(m_k+3)r^2} (Q(m_k+1)L^{m_k+1})^{\frac{2}{m+3}}}{2\log[2]} (m_k+3) \\ &\quad \left( t_{max}^{-\frac{1}{m_k+3}} \left( -3 - m_k + (3+m_k)_2 F_1 \left[ 1, -\frac{1}{m_k+3}, \frac{m_k+2}{m_k+3}, -t_{max} \frac{P_r}{\sigma_d^2} \right] - \log \left[ 1 + t_{max} \frac{P_r}{\sigma_d^2} \right] \right) \right. \\ &\quad \left. - t_{min}^{-\frac{1}{m_k+3}} \left( -3 - m_k + (3+m_k)_2 F_1 \left[ 1, -\frac{1}{m_k+3}, \frac{m_k+2}{m_k+3}, -t_{min} \frac{P_r}{\sigma_d^2} \right] - \log \left[ 1 + t_{min} \frac{P_r}{\sigma_d^2} \right] \right) \right). \quad (17) \end{aligned}$$

$m_k$  is the order of the Lambertian radiation pattern which is given by

$$m_k = \frac{-1}{\log_2(\cos(\phi/2))}, \quad (10)$$

where  $\phi/2$  denotes the semi-angle of the LED.

To simplify our analysis, let us assume that  $Q = \frac{1}{2\pi} A_d U(\Psi_K) g(\Psi_K) R_p$ . Hence, (9) can be rewritten as

$$h_v = \frac{Q(m_k+1)L^{m+1}}{(r_k^2 + L^2)^{\frac{m+3}{2}}}. \quad (11)$$

It is assumed that the location of the users is uniformly distributed with PDF given as

$$f_{r_k}(r) = \frac{2r}{r^2}. \quad (12)$$

The PDF of the un-ordered channel gain of the VLC link can be driven using the change-of-variable method used in [5] as follows

$$f_{h_k}(h) = \left| \frac{\partial}{\partial h} u^{-1}(h) \right| f_{h_k}(u^{-1}(h)). \quad (13)$$

We can now derive the PDF of the VLC channel gain given by

$$f_{h_k} = \frac{2Q^{\frac{2}{2+m}} ((m_k+1)L^{m_k+1})^{\frac{2}{m+3}} h^{-\frac{2}{m_k+3}-1}}{(m_k+3)r^2}, \quad (14)$$

where  $r$  is the maximum cell radius of the LOS.

The PDF of  $h_k^2$  can now be obtained as

$$f_{h_k^2} = \frac{-Q^{\frac{2}{2+m}} ((m_k+1)L^{m_k+1})^{\frac{2}{m+3}} h^{-\frac{m_k+4}{m_k+3}} h^{\frac{1}{m_k+3}}}{(m_k+3)r^2}. \quad (15)$$

Substituting (7) and (15) in (8), we obtain (16), shown at the top of the next page,

Substituting  $t_{min}$ ,  $t_{max}$  values in (16) we obtain (17), shown at the top of the next page.

## B. Outage Probability

The outage probability is simply defined as the probability that the instantaneous SNR of system is less than a certain threshold value,  $R_{th}$ , and is given as

$$P_{outage} = P_r [C < R_{th}]. \quad (18)$$

The end-to-end outage probability for the proposed system can be written as

$$P_{outage} = P_{out}^{PLC} + (1 - P_{out}^{PLC}) P_{out}^{VLC}, \quad (19)$$

where  $P_{out}^{PLC}$  is outage probability of the first link and  $P_{out}^{VLC}$  is the outage probability of the second link.

The cumulative density function (CDF) of each link represents the outage probability of that link. Therefore, the outage probability of the PLC and VLC links can be calculated as

$$P_{out}^{PLC} = \int_0^\infty \frac{\zeta}{z\sqrt{8\pi\sigma}} \exp \left( -\frac{(\zeta \ln(\gamma) - (2\mu + \zeta \ln(a_1)))^2}{8\sigma^2} \right) dz, \quad (20)$$

and

$$P_{out}^{VLC} = \frac{-1}{r^2} ((m_k+1)QL^{m_k+1})^{\frac{2}{m_k+3}} h^{\frac{-1}{m_k+3}} + \left( 1 + \frac{L^2}{r^2} \right). \quad (21)$$

## IV. NUMERICAL RESULTS

This section presents some numerical results of the derived expressions above. The system parameters under consideration are, unless indicated otherwise, as follows: operating frequency of the system  $f = 500\text{kHz}$ ,  $k = 0.7$ ,  $a_0 = 2.03 \times 10^{-3}$ ,  $a_1 = 3.75 \times 10^{-7}$ ,  $d_1 = 30\text{m}$ , the input power  $P_s = 0.1\text{W}$ ,  $P_r = 0.1\text{W}$ , input SNR is 10dB,  $A_d = 0.1\text{m}$ ,  $U(\Psi_K) = g(\Psi_K) = 7\text{dB}$ ,  $R_p = 0.4\text{A/W}$ ,  $r = 3.6\text{m}$ ,  $L = 2.15\text{m}$  and  $\phi/2 = 60^\circ$  [15].

The effect of the relay transmit power and the vertical distance to the user plane on the performance of the proposed hybrid system is presented in Fig. 2. It is clear that the analytical results, obtained from (17), are in perfect agreement with the simulation ones. As it can be seen, the performance

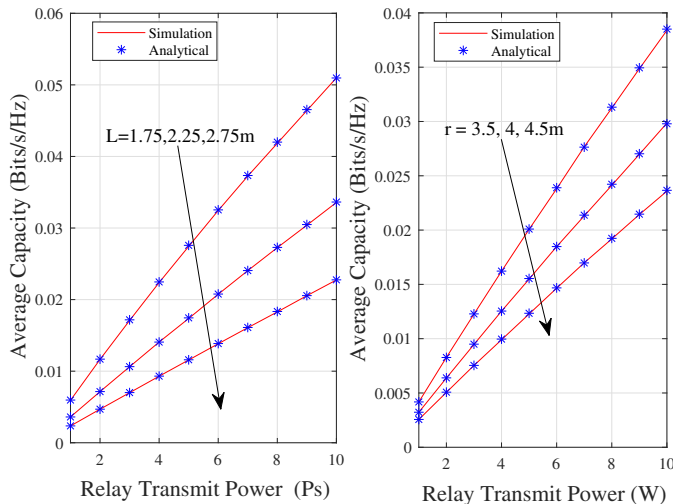


Fig. 2: Average capacity as a function of relay transmit power for different values of the vertical distance to the user plane.

Fig. 3: Average capacity with respect to the relay transmit power for different values of the maximum cell radius of the LOS.

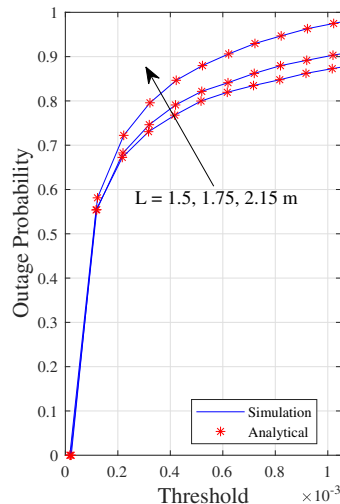


Fig. 4: Outage probability versus the threshold value for different values of the vertical distance to the user plane.

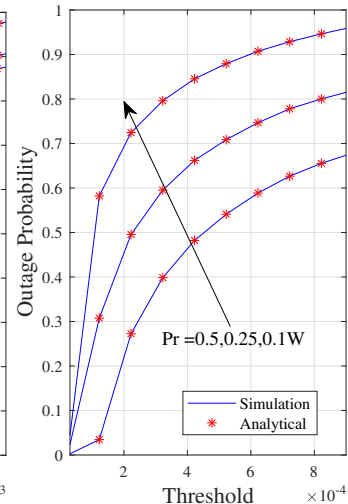


Fig. 5: Outage probability versus the threshold value for different values of relay transmit power.

improves as the relay transmit power increases and/or the vertical distance of the LED decreases. Fig. 3 illustrates the impact of the maximum cell radius of the LOS on the system performance. It is noticeable that the performance of the system has a noticeable improvement when the maximum cell radius of the LOS decreases, particularly for the high values of the relay transmit power.

The outage probability of the proposed system is plotted in Figs. 4 and 5 versus the threshold for different values of the height of the LED and the relay transmit power, respectively. Looking at both figures, we can see that the performance is considerably affected by these two factors as it degrades when the relay transmit power increases and the vertical distance decreases. On the other hand, it increases when the relay transmit power declines and the height of the LED increases.

## V. CONCLUSIONS

This paper analyzed the performance of the hybrid PLC/VLC system in terms of the average capacity and outage probability for which analytical expressions were derived and then verified by Monte Carlo simulations. We investigated the effect of different system parameters on the performance of the proposed system. The results revealed that the performance of the proposed hybrid system is affected by various parameters, such as the relay transmit power, the height of the LED and the maximum cell radius of the LOS. It is worth pointing out that the use of such hybrid systems can provide better mobility to the end user than that provided by the PLC-only system.

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