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SHEAR BEHAVIOUR OF LIGHTWEIGHT CONCRETE BEAMS STRENGTHENED WITH CFRP COMPOSITE

Mustafa Hameed Al-Allaf¹, Laurence Weekes² and Levingshan Augusthus-Nelson²

¹ University of Al-Nahrain, Baghdad, Iraq

² School of Computing Science and Engineering, University of Salford, M5 4WT, United Kingdom

ABSTRACT

This paper presents the experimental results obtained from lightweight and normal concrete beams with closed and U-shaped configurations of epoxy bonded Carbon FRP (CFRP) reinforcement in order to compare the shear resisting mechanisms between lightweight and normal concrete beams. The experimental results show that the CFRP can successfully be applied in the strengthening of lightweight concrete beams and the shear strength gained due to CFRP reinforcement for lightweight samples is less than the normal weight concrete samples while the mode of failures are the same. In contrast, diagonal shear cracks propagate through the lightweight aggregate compared to cracks around normal aggregate in the concrete matrix. Furthermore, the numerical study shows that the design guidelines to estimate the CFRP contribution, which do not differentiate the concrete types, overestimate the U-shaped CFRP contribution on lightweight concrete beams where the effective bond length of CFRP could not be achieved due to lower tensile strength of lightweight concrete.

Keywords: Buildings, structures & design; Composite structures; Concrete structures.

List of Notations

A_f	Area of CFRP strap
E_f	Modulus of elasticity of CFRP strap
ϵ_f	Strain on CFRP strap
V_f	Shear resistance by CFRP straps
V_t	Total shear capacity
V_c	Shear resistance by concrete

24 INTRODUCTION

25 Lightweight aggregates, Pulverised Fuel Ash (Lytag, 2011), instead of coarse granite
26 aggregates have been used in concrete structural elements. The dead weight of concrete
27 elements are significantly reduced due to lightweight aggregate and the geometric shape of an
28 element cast with lightweight concrete can be increased without increasing its weight. In the
29 coming decades, it is, therefore expected that structures constructed using lightweight
30 concrete will occupy a significant proportion of concrete infrastructures.

31 Lightweight concrete structures are worse affected by deterioration than normal weight
32 structures. This is due to permanent deterioration of concrete materials, applied load more
33 than envisaged design load and lack of understanding in behaviour of lightweight concrete as
34 a structural material. The deteriorated lightweight concrete structures may be retrofitted to
35 reduce the economic impact rather than replace with new structures. Thus, recent studies as
36 recommended in ACI 440.2R (2008) have been directed to investigate efficient strengthening
37 systems such as near surface mounted and epoxy bonded steel or FRP reinforcements in
38 lightweight concrete structures.

39 Shear failure in normal concrete is a controversial topic among structural engineers (Kim and
40 Sebastian, 2002; Sundaraja and Rajamohan, 2009; Zhang, 1997; You et al., 2017). This
41 disparity is because the different design guidelines suggest various relative contribution of
42 shear carrying mechanisms such as aggregate interlock, friction between the shear cracks,
43 dowel action by longitudinal reinforcement, and contribution to the compression zone and
44 vertical resistance by shear links. Hence, there is no single universal design method accepted
45 in different parts of the world. When it comes to retrofitted systems with FRP, variability in
46 materials and bond properties add to the complication in design guidelines. This problem is
47 further amplified due to the lack of aggregate interlock and weaker tensile strength in

48 lightweight concrete. In order to simplify the design guidelines for lightweight concrete, the
49 shear capacity is treated in a similar manner to normal concrete with reduction factors both
50 with and without a retrofitted system.

51 Externally bonded fibre reinforced polymer (FRP) plates or sheets have proved to be a better
52 retrofitting system for reinforced concrete (RC) structures compared to traditional
53 strengthening techniques. FRP has good corrosion resistance, is lightweight and has excellent
54 mechanical properties. Furthermore, the manual strengthening system allows using the FRP
55 reinforcements to any member's shape. A significant amount of research has been conducted
56 to investigate the shear behaviour of normal weight concrete beams strengthened with FRP
57 composites, including the influence of the strengthening configurations and the bonded length
58 of the FRP reinforcement (Triantafillou, 1998; Adhikary et al., 2004), shear span to depth
59 ratio (Khalifa and Nanni, 2002; Lee et al., 2011), size effect (Leung et al., 2007; Foster et al.,
60 2016), shear reinforcement ratio (Pellegrino and Modena, 2002), the orientation and the
61 width of the FRP reinforcement (Monti and Liotta, 2007; Sundaraja and Rajamohan, 2009;
62 Mofidi and Chaallal, 2011), and type of loading (Anil, 2006 and 2008; Carolin and Täljsten,
63 2005). However, the study of the response of lightweight concrete (LWC) beams
64 strengthened in shear with reinforcement has not received much attention. Hence, ACI
65 440.2R (2008) suggests further investigation of the effect of FRP on lightweight concrete.

66 In order to understand the local bond behaviour between the FRP reinforcement and
67 lightweight concrete, experimental investigation of double-lap shear specimens were
68 conducted by Al-Allaf et al. (2016). The test results showed that the LWC concrete has a
69 lower bond strength compared to NWC. It is envisaged that the strengthening of LWC
70 members will be the significant challenge for structural engineers in the coming decades. In
71 this paper, therefore, epoxy bonded CFRP strengthening techniques in LWC beams are

72 studied along with NWC in order to verify the shear reduction factors suggested by existing
73 design guidelines and numerical models, which were developed for NWC.

74 **EXPERIMENTAL INVESTIGATION**

75 This study focusses on the behaviour of LWC beams externally strengthened in shear using
76 carbon fibre reinforced polymers (CFRP) strips. Identical LWC and NWC beams were
77 prepared and tested under monotonic loading conditions in order to compare the
78 strengthening techniques and shear resisting mechanisms between LWC and NWC beams.

79 **SPECIMEN DESIGN**

80 The entire experimental program comprised six specimens cast with lightweight and normal
81 weight concretes. Both the NWC and LWC beams were geometrically similar and cast using
82 the same grade of concrete (i.e. the same compressive strength). The details of each series are
83 as follows:

- 84 • Series **(BL-UST/CST)** comprised three beams cast with LWC without shear
85 reinforcement except two shear links adjacent to the supports; one of the beams was
86 without external CFRP reinforcement and the remaining two beams were each
87 strengthened with U-shaped (UST) and close (CST) epoxy bonded external CFRP strips.
- 88 • Series **(BN-UST/CST)** comprised three companion beams cast with NWC without shear
89 reinforcement except two shear links adjacent to supports either side; one beam was used
90 as a control beam without CFRP reinforcement and two beams were strengthened with
91 CFRP similar to the LWC beams.

92 All the reinforced LWC and NWC beams were designed to have the same dimensions of 200
93 mm wide by 300 mm deep and 2000 mm long as shown in Figure 1. The simply supported
94 beams were loaded under four-point loading conditions with supports located at a distance of

150 mm from the both ends of the beam. Displacement controlled monotonic loading conditions were employed. The shear span to effective depth ratio was taken as $a/d=2.27$ to secure shear failure which satisfies the definition of a shear beam (Kani, 1966). All the beams were reinforced for flexure with three bottom and two top 16 mm diameter longitudinal deformed steel reinforcing bars (H16 steel bar). The longitudinal steel ratio for both top and bottom reinforcement for all beams was 1.67%. The flexural steel reinforcement was detailed to ensure shear failure of the samples strengthened with CFRP. The effective depth of the beam and the clear cover distance were 264 mm and 28 mm respectively.

103 **CONFIGURATION OF CFRP REINFORCEMENT**

104 CFRP reinforcement was used in this test with various shear strengthening systems as
 105 illustrated in Table 1. Closed-shaped CFRP reinforcements were attached as strips on all the
 106 faces of the beam. Also, U-shaped systems were attached on the tension (bottom) and the two
 107 side faces of the beam as strips. The CFRP reinforcements were orientated at 90^0 with respect
 108 to the longitudinal axis of the beam as shown in Figure 2. The width of CFRP reinforcement
 109 was 100 mm and the spacing of 150 mm from centre-to-centre of the attached CFRP strips.
 110 These CFRP reinforcements were attached along the shear span of the beam, from the
 111 support point up to the point of load application on both sides of the beam.

112 **Table1: Summary of test parameters**

Sample	CFRP ratio (%)	CFRP strengthening type	CFRP orientation	CFRP wrap coverage
BL	0	-	-	-
BL- UST	0.0785	U-shaped	90^0	Strip
BL- CST	0.0785	Closed-shaped	90^0	Strip
BN	0	-	-	-
BN- UST	0.0785	U-shaped	90^0	Strip
BN- CST	0.0785	Closed-shaped	90^0	Strip

113

114 MATERIAL PROPERTIES

115 Pulverised Fuel Ash (Lyttag) instead of coarse aggregates were used in the preparation of the
116 lightweight concrete mixture. The particle size grading, physical properties and chemical
117 composition of the Lytag aggregates are reported by Al-Allaf et al. (2016). The concrete
118 mixes for both concrete types were designed to have a slump of 75 mm, and a 28-day cube
119 compressive strength of 40 N/mm². The mix details for the lightweight and normal weight
120 concretes are given in Table 2. All the LWC and NWC samples were cast in a single batch
121 each. Furthermore, a total of 18 concrete cubes (100 x 100 x 100 mm), eight concrete
122 cylinders (150 dia. x 300 mm) and six prisms (100 x 100 x 400 mm) were cast from each
123 batch to determine the uniaxial compressive strength, the Young's modulus of elasticity, the
124 concrete density and the modulus of rupture of lightweight and normal weight concretes (see
125 Table 3).

126 Table 2: The mix design of lightweight and normal weight concretes

Concrete type	Water (kg)	Cement (kg)	Sand (kg)	Coarse aggregate (kg)	Design strength (N/mm ²)
NWC	192	400	667	1184	40
LWC	216*	480	485	715	40
* The moisture content and absorption of lightweight aggregates were considered in calculations of mix design.					

127

128 Table 3: Mechanical properties of concretes

Concrete type	Average concrete compressive strength (MPa)	Average modulus of rupture (MPa)	Average modulus of elasticity (MPa)	Average concrete density (kg/m ³)
NWC	42.1	3.49	29860	2356
LWC	43.34	3.026	23510	1823

129

130 For steel reinforcing bars, three samples of longitudinal bars were tested in uniaxial tension.
 131 Average properties of steel reinforcement are listed in Table 4.

132 Table 4: Mechanical properties of 16 mm diameter steel bar

Yield stress (MPa)	Yield strain ($\mu\text{m/m}$)	Ultimate stress (MPa)	Ultimate strain (mm/m)	Modulus of elasticity (GPa)
510	2600	650	130000	200

133
 134 Mechanical properties of the unidirectional CFRP sheets (C Sheet 240) and primer resin are
 135 summarised in Table 5 (Weber UK, 2008). Epoxy plus primer (EN-Force primer) and epoxy
 136 plus adhesive (EN-Force bonding adhesive) were used to bond the CFRP composite to the
 137 surface of the concrete. Two-thirds of the adhesive as the base component and one-third of
 138 hardener were used according to the manufacturer's recommendations.

139 Table 5: Mechanical properties of the CFRP sheet and the primer resin (Weber UK, 2008)

CFRP sheet	
Modulus of elasticity	240 GPa
Tensile strength	4000 MPa
Strain at failure	1.6%
Primer resin	
Compressive strength	100 N/mm ²
Tensile strength	19 N/mm ²
Flexural strength	30 N/mm ²
Bond to concrete	> 5.3 N/mm ²
Modulus of elasticity	5 kN/mm ²

141
 142 A concrete grinder machine was used to smooth the surface of the concrete in order to
 143 achieve the required level of stress transference between the CFRP and the surface of the
 144 concrete. Then, the surface was cleaned to remove the dust produced during the grinding
 145 process. Samples corners were rounded to prevent unwanted CFRP rupture which can be
 146 developed as a result of the high-stress concentration in the CFRP reinforcement wrapped

147 close the corner of the beam. For the U-shaped systems, the CFRP reinforcement was
148 attached directly below the top surface of the beams by approximately 20 mm.

149

150 **TEST ARRANGEMENT**

151 The four-point loading arrangement shown in Figure 3 was used. A 500 kN load cell attached
152 to a hydraulic jack was used to record the applied load during the test, with monotonic loads
153 applied via a spreader beam. This spreader beam was seated on 25 mm diameter steel rollers
154 welded to steel plates (length=200 mm and width=100 mm) bedded on the top surface of the
155 sample to avoid local crushing of concrete at the load point. The sample is placed over the
156 two support points with a 25 mm diameter steel roller seated on the top surface of a 100 mm
157 steel plate. One of the steel rollers was welded to the steel plate, and a (length=200 mm and
158 width=100 mm) steel plate was provided on top of the roller to avoid local crushing of
159 concrete at the support as shown in Figure 3.

160 **INSTRUMENTATION**

161 **Steel Strain Gauges**

162 Ten FLA-6-11 uni-directional strain gauges by Tokyo Sokki Company were used to record
163 the strain measurements at different positions along the length of the middle bar in the bottom
164 layer in each of the normal and lightweight samples. The gauge factor, gauge resistance and
165 the gauge length were 2.12 ± 1 %, 120 ± 0.5 Ω and 6 mm respectively. Strain gauges were
166 positioned externally at 250 mm, 400 mm, 550 mm, 700 mm, and 850 mm from both ends of
167 each beam, as shown in Figure 4. The gauges were denoted as “LS” combined with a number
168 starting from 1 to 10 to identify their location from the left end of the beam.

169 **CFRP Strain Gauges**

170 Figure 5 illustrates the strain gauges employed in the CFRP reinforcement during the test.
171 The strain gauges and CFRP strip were denoted as “SG” and “SF” respectively. The type
172 FLA-5-11 strain gauge by Tokyo Sokki Company measures a uni-directional strain, which
173 was orientated vertically and has a gauge factor and length of 2.12% and 5 mm respectively.
174 The same arrangements were employed for all LWC and NWC strengthened samples.

175 **Linear Variable Differential Transformers (LVDTs)**

176 Three Linear Voltage Displacement Transducers (LVDTs) were used in this test to record
177 vertical deflections at various positions along the sample as shown in Figure 6. The LVDTs
178 were mounted on a frame connected to the centre of concrete directly above the supports to
179 measure the relative displacement along the beams.

180 **EXPERIMENTAL RESULTS**

181 A summary of the samples shear strength based on the maximum shear carrying capacity, the
182 recorded mid-span deflection and the modes of failure are summarised in Table 8.

183 Table 8: Summary of the shear capacities, failure deflection and modes of failure

Sample	Max Shear capacity (kN)	Mid-span Deflection at failure (mm)	Failure mode, CFRP failure
BL	151.78	4.82	Failure in shear
BL-UST	218.38	7.10	Failure in shear due to CFRP debonding
BL-CST	267.14	11.3	Failure in shear due to CFRP rupture
BN	164.1	5.35	Failure in shear
BN-UST	248.6	7.69	Failure in shear due to CFRP debonding
BN-CST	320.8	10.3	Failure in shear due to CFRP rupture

184
185 Comparison of the maximum shear failure loads between CFRP-retrofitted samples and the
186 reference sample reveals that the CFRP retrofitting systems were efficient in improving the

187 shear strength of the LWC and NWC beams. Figure 7(a) shows the shear strength gained due
188 to CFRP reinforcement in the strengthened samples compared with the corresponding control
189 samples of LWC and NWC. For the LWC series, the shear strength provided by CFRP
190 reinforcement for U-shaped and Closed-shaped samples were 44% and 76% respectively,
191 when compared with the control sample, while for the NWC series, the shear strength
192 provided by CFRP reinforcement for U-shaped and Closed-shaped samples were 51% and
193 95% respectively.

194 In this study, the shear strength of the control, U- shaped and Closed-shaped samples of LWC
195 are 92%, 87% and 83% of the control, U-shaped and Closed-shaped samples of the
196 corresponding NWC samples respectively.

197 All the strengthened samples demonstrate increases in the maximum deflection over the
198 control samples at failure as shown in Figure 7(b) and Table 8. LWC and NWC samples
199 strengthened with U- shaped CFRP had 47% and 43% greater maximum deflection at failure
200 over the control LWC and NWC samples. Comparison with samples strengthened with
201 Closed-shaped CFRP had an increase in maximum deflection at failure of 134% and 93%
202 respectively. This observation resulted from the evidence that crack bridging forces provided
203 by CFRP reinforcements could increase the shear strength of LWC and NWC beams and
204 yielded a better ductility over the control samples. In contrast, LWC samples demonstrated
205 lower shear enhancement while producing higher ductile behaviour compared to
206 corresponding NWC samples. Increases in interfacial and shear stresses with increasing
207 plastic deformation leads to CFRP debonding and unexpected CFRP rupture failures, thus the
208 effectiveness of FRP for shear strengthening LWC beams will be affected by this issue. This
209 observation can be attributed to a lower concrete surface tensile strength, aggregate interlock
210 at the diagonal crack faces and requirement for longer effective bond length in LWC as
211 observed by Al-Allaf et al. (2016 and 2015). CFRP bond deterioration in LWC requires

212 consideration to ensure the safety of CFRP applications for shear strengthening of LWC
213 beams.

214 **LOAD-DEFLECTION RESPONSE**

215 The shear-deflection response curves for all the specimens are compared in Figure 8. The
216 behaviour trends for NWC and LWC samples are described by three zones of stiffness's: (i)
217 elastic stiffness zone (elastic behaviour), (ii) flexural stiffness zone, and (iii) shear stiffness
218 zone. In general, all LWC and NWC beams showed the same elastic stiffness zone before
219 first flexural cracks (approximately 50 kN). The flexural stiffness zone showed the same
220 linear trend until a diagonal crack appeared at the surface of concrete at the applied load
221 between 100-130 kN load range for NWC beams and 90-120 kN load range for LWC beams.

222 As illustrated in Figure 8, the lightweight control sample (BL) reached a maximum load of
223 151.78 kN and corresponding mid-span deflection of 4.30 mm. An abrupt increase in applied
224 load developed at this stage as a result of the diagonal shear crack opening width. The
225 strengthened LWC samples (BL-UST and BL-CST) exhibit identical stiffness at low level
226 loading. This can be attributed to the configuration of the CFRP which would not influence
227 the stiffness until the diagonal shear crack developed. However, at the maximum load for
228 Closed-shaped samples, the shear cracking zone was considerably higher than those observed
229 in the samples with the U-shaped system. This is assigned to the premature failure for
230 samples strengthened with the U-shaped system where effective length of CFRP bond was
231 not available. It can be noticed that the NWC samples displayed similar shear deflection
232 shapes to the corresponding LWC samples.

233 Figure 8 also shows that the stiffness of LWC samples is lower than those of NWC samples
234 with identical CFRP strengthening configurations after initial cracking. This behaviour is a
235 result of the variance in rigidities of the LWC tested samples. LWC samples had lower

236 stiffness compared with NWC samples due to lower stiffness of lightweight aggregate
 237 (LWA) particles and higher cement ratio (Clarke, 2002).
 238 Both controlled and U-shaped LWC and NWC samples (BL, BN, BL-UST and BN-UST)
 239 failed immediately after reaching the maximum load carrying capacity. This is due to the fact
 240 that the crack bridging force across the diagonal crack was not available or fully reached its
 241 capacity in the controlled and U-shaped retrofitted systems respectively. However, both
 242 closed-shaped LWC and NWC samples (BL-CST and BN-CST) exhibited a plastic behaviour
 243 before the rupture of CFRP sheets.

244 FAILURE MODES

245 All the tested LWC and NWC beams failed in shear by initiation of diagonal tension cracks
 246 in the shear span. Loss of friction at the crack interfaces and shear rotation were the failure
 247 modes of the control samples. In the case of samples retrofitted with CFRP reinforcements,
 248 the CFRP strips either debonded or ruptured as shown in Figure 9. The inclinations of
 249 diagonal tension shear cracks are summarised in Table 9, which are numbered from 1 to 3
 250 according to their location from the left end of the beam. In general, the orientation of the
 251 diagonal tension crack for strengthened samples was lower than their corresponding control
 252 samples. Furthermore, there is no variance in response between corresponding lightweight
 253 and normal weight samples regarding the inclinations of diagonal shear cracks despite the
 254 clear difference in ultimate shear loads.

255 Table 9: Inclination of diagonal shear cracks

Sample	Inclination of diagonal shear cracks			Average inclination
	θ_1	θ_2	θ_3	
BL	42 ⁰	40 ⁰		41 ⁰
BL-UST	34 ⁰	30 ⁰		32 ⁰
BL-CST	33 ⁰	37 ⁰	35 ⁰	35 ⁰
BN	41 ⁰	44 ⁰		42 ⁰
BN-UST	33 ⁰			33 ⁰
BN-CST	35 ⁰	37 ⁰	34 ⁰	35 ⁰

256

257 The CFRP reinforcements have significant effects on the beams crack distributions. The
258 CFRP reinforcements delay the loss of friction by reducing the diagonal crack opening width.
259 This was achieved by the confinement and crack bridging effects of CFRP. At the ultimate
260 limit state, the crack bridging effect was lost and the loss of friction occurred suddenly
261 without any warning. The failure patterns are extremely brittle when compared to the control
262 samples. The same failure modes were observed by Bousselham & Chaallal (2008).

263 Shear failure as a result of CFRP debonding was the failure mode of the LWC sample
264 strengthened with U-shaped CFRP (BL-UST). The failure in bond between CFRP and
265 concrete was initiated by debonding in a thick layer of lightweight concrete close the surface
266 of the beam, (see Figure 9(c)). The CFRP reinforcement was detached locally from the
267 surface of concrete at the diagonal shear cracks. With more loading, the debonding failure
268 gradually extended from the crack and moved away towards the top and the bottom of the
269 beam. A similar failure mode was observed for the NWC sample strengthened with U-shaped
270 CFRP (BN-UST) except the CFRP debonding initiated with a thin layer of normal concrete
271 (close to the concrete surface)(see Figure 9(d)). Generally, BL-UST showed higher crack
272 intensity and widths compared with BN-UST. The average major diagonal crack widths in
273 BL-UST and BN-UST were about 7 and 4 mm respectively.

274

275 In contrast, LWC and NWC samples strengthened with Closed-shaped CFRP (BL-CST and
276 BN-CST) failed due to CFRP rupture (see Figure 9(e) and (f)). CFRP fibres across the
277 diagonal shear crack snapped one-by-one because of excessive straining. These samples also
278 failed in extremely brittle manner compared with the control samples. Furthermore, CFRP
279 rupture caused larger increases in shear strength compared to CFRP debonding failure. This
280 can be attributed to longer effective bond length in the Closed-shaped CFRP. Each of the

281 samples had few diagonal shear cracks. However, no significant difference in the crack
282 pattern was observed between lightweight and normal weight samples. Furthermore, the
283 failures of the samples were due to a single diagonal crack. The average major diagonal crack
284 widths in BL-CST and BN-CST were about 4 and 3 mm respectively.

285 It was noticed that the LWC samples exhibited low shear strengths and weaker friction
286 between crack faces. In this study, microstructural examinations using a light microscope and
287 a scanning electron microscope (SEM) were conducted on a sample of lightweight and
288 normal weight concrete collected from the crack faces in order to examine the macro/micro
289 and nano internal pore structures. These methods were implemented to support the behaviour
290 observed in the disruptive failure test. Interestingly, light micrographs of lightweight concrete
291 samples show that the path of diagonal tension cracks propagated through the lightweight
292 aggregates (see Figure 10 (a)) rather than in the concrete matrix around the aggregates as in
293 normal weight samples (see Figure 11 (a)). This could be attributed to the lower tensile
294 strength of lightweight aggregate compare to normal weight aggregate. Hence, it can be
295 concluded that the energy required for the crack opening through the lightweight aggregates
296 is less than the crack propagation around the coarse aggregates. Due to the cracks though the
297 aggregates, the crack faces do not have a significant amount to surface interlock, which is
298 common in normal weight concrete. Therefore, the aggregate interlock between the crack
299 faces could be neglected in lightweight concrete beams and this eventually leads to the lower
300 shear capacity of lightweight concrete beams.

301 The SEM micrographs of the lightweight concrete sample revealed the spherical shapes of
302 Lytag particles with an extremely porous microstructure (see Figure 10 (b) to (e)). In contrast,
303 the normal weight aggregates are angular in shape with a non-porous surface (see Figure 11
304 (c)). Furthermore, the lightweight aggregate is surrounded by an orange coloured area
305 (reacted zone) (see Figure 10 (a)). This is due to the chemical reaction between the

306 lightweight particles and the cement matrix. Figure 10 (c) shows the reacted zone and the
307 microstructure of lightweight particles, in which the voids are considerably higher than the
308 cement paste. Also, Figure 10 (d) illustrates the boundary between the reacted zone and the
309 cement paste. It can also be observed that the cement paste and lightweight particles are well
310 interlocked as illustrated in the typical microstructure of the interfacial zone for a composite
311 of Lytag particle and cement paste (see Figure 10 (a)).

312 Figures 11(b) and (d) show that the normal aggregates are bonded with the cement paste
313 rigidly and cracks develop around the aggregates. In this case the aggregate interlock between
314 the crack faces potentially provides significant contribution to the ultimate shear carrying
315 capacity.

316 **LONGITUDINAL STEEL STRAIN**

317 The longitudinal steel reinforcement was slightly strained at the earlier stage of loading and
318 starts to elongate with the occurrence of flexural or shear cracks. Yielding of the central steel
319 bar was not observed in the control normal and lightweight samples due to premature shear
320 failure. Furthermore, it was noted that the tested samples showed approximately the same
321 elongations at a low level of loading on both sides of the LWC and NWC samples.
322 Longitudinal steel strain profiles of samples BL-CST and BN-CST at various load levels
323 (20%, 40%, 60%, 80%, and 100% of the maximum shear capacity) are presented in Figure
324 12, where the horizontal black line represents the yield strain of the steel. Variance in strain
325 measurements was noticed at a higher level of loading in several samples, which can be
326 attributed to the position, number and effect of diagonal shear and flexural cracks. For BL-
327 CST, the recorded strains close to the centre of the beam are lower compared with
328 corresponding BN-CST, except at the ultimate load (100%) as shown in Figure 12 (a) and
329 (b). Similar behaviour was observed between the BL-UST and BN-UST samples. This
330 behaviour can be attributed to the multiple hair-line flexural cracks observed in the middle of

331 the beam and initiation of shear cracks close to the applied load for the normal weight
332 concrete samples. In contrast, diagonal shear cracks close to support in lightweight concrete
333 samples were prevalent. The strain distributions at the ultimate load of both LWC and NWC
334 samples were similar. Hence, the contribution of dowel action by longitudinal reinforcement
335 for shear resistance in LWC and NWC samples could be considered as the same at the
336 ultimate load (Martin-Perez and Pantazopoulou, 2001).

337 **CFRP STRAIN**

338 The average strain response of CFRP reinforcement is characterised by two stages: the first
339 stage is where the CFRP strains are very small and the second stage where an abrupt increase
340 of CFRP strains develops with further loading. The first considerable increase in CFRP
341 strains developed at an applied load of 100 kN for BL-UST, 120 kN for BL-CST, 110 kN for
342 BN-UST and 130 kN for BN-CST. It can be noted that the LWC samples has a slightly lower
343 applied load at the point of shear crack initiation. This observation was related to the crack
344 propagation across the CFRP strips. This crack would subsequently initiate into the diagonal
345 shear crack that could lead to failure of the sample. Up to this loading point (initial crack
346 load), the contribution of the CFRP reinforcement to the total shear strength of the reinforced
347 concrete beam is very small and can be ignored. With further loading, the crack opening
348 increases and new shear cracks develop, leading to an increase in CFRP stress due to crack
349 bridging forces of the CFRP strips. The sudden decrease in CFRP strains which is observed at
350 higher level of loading in some of the instrumented CFRP strips for samples with U-shaped
351 reinforcement. This is could be attributed to the global debonding of the CFRP reinforcement
352 from the surface of the concrete.

353 The CFRP strains of all the effective straps at the failure loads are summarised in Table 10. A
354 significant difference in measured CFRP strains between U-shaped and Closed-shaped
355 samples were observed. This is attributed to the premature failure of samples with the U-

356 shaped strengthening technique. Samples with Closed-shaped CFRP reinforcement were able
357 to sustain larger strains compared with U-shaped samples.

358 Generally, the stress distribution in the RC beam is complex and may affect the CFRP-to-
359 concrete interface, with an expectation to accelerate CFRP debonding and to minimise the
360 maximum debonding strain. The increase in interfacial and normal stresses with increasing
361 plastic deformation in lightweight concrete beams leads to unexpected CFRP reinforcement
362 failures and thus a reduction in the maximum debonding strains.

363 Table 10: Summary of maximum local CFRP strains at sample failure

Sample	Shear force (kN)	Strains at failure from individual gauges at each instrumented CFRP strips ($\mu\text{m}/\text{m}$)					
		SF1	SF2	SF3	SF4	SF5	SF6
BL-UST	218.4	4011.6	4725.9	2911.0	4728.6	4216.7	1662.4
BL-CST	267.1	5819.4	5972.5	4800.3	2788.3	4466.5	1846.8
BN-UST	248.6	2120.8	5837.5	664.5	1642.6	846.1	4919.4
BN-CST	320.8	2393.0	9416.0	7893.2	2579.8	1948.1	4711.9

364 NUMERICAL ANALYSIS

365 SHEAR COMPONENT ANALYSIS

366 The shear contribution of CFRP was calculated using two different methods. Firstly the
367 subtraction method allows the calculation of the shear contribution provided by the concrete
368 and CFRP reinforcements using the difference in failure loads between samples, which is
369 useful in understanding the efficiency of CFRP reinforcement. This method is derived based
370 on the concept that the shear contribution by the additional confinement effect of concrete in
371 the presence of CFRP at failure load could be negligible (Khalifa and Nanni, 2002). This
372 method can be illustrated using a simple free-body diagram of half of the cracked beam as
373 shown in Figure 13.

374 Secondly, the shear contribution of the CFRP strips can be evaluated by summing the
375 contribution provided by CFRP reinforcement across the diagonal shear crack at each side of
376 the beam, as shown in Equation 1:

$$V_f = \sum_{i=1}^n A_{fi} E_f \varepsilon_{fi} \quad (1)$$

377 where V_f is the estimated shear force provided by the CFRP reinforcement, A_f is the area of
378 the CFRP strip, E_f is the elastic modulus of CFRP material, ε_f is the strain determined from
379 strain gauges attached to the CFRP strip and n is the number of stirrups or CFRP strips
380 crossing the observed critical shear crack,. The relative contribution of shear resistance by
381 various mechanisms (i.e., tensile strength of concrete, aggregate interlock at the diagonal
382 crack faces, compressive strength of concrete, interfacial shear stress, dowel action provided
383 by the longitudinal steel reinforcement) were not fully understood so far (Kim, 2011). Hence,
384 the shear contributions of these mechanisms of concrete beam with longitudinal
385 reinforcement were considered together in this study. The concrete contribution (V_c) was
386

387 obtained by subtracting the estimated contributions of CFRP reinforcement (V_f) from the
388 total shear capacity at a particular load level (V_t) as given by Equation (2):

$$V_c = V_t - V_f \quad (2)$$

389
390 Figure 14 shows the results of the shear component analysis for the LWC and NWC beam
391 specimens. In these figures, the horizontal axis represents the total applied load recorded by
392 the load cell and the vertical axis represents the total shear contribution of concrete and CFRP
393 reinforcements on both sides of the beam. It can be noted that the shear strength provided by
394 CFRP reinforcement was very small and can be ignored before the occurrence of a diagonal
395 shear crack. In this stage, external loads applied to the samples are mainly resisted by the
396 concrete. As the diagonal shear crack develops, a part of the load is taken by the CFRP
397 reinforcement as demonstrated by a sudden leap in the CFRP shear contribution response
398 curves. The CFRP reinforcement gradually carries the external shear force until the CFRP
399 reinforcement detaches from the surface of the concrete or ruptured. Abrupt falls in the CFRP
400 shear contribution can be highlighted when the CFRP reinforcement debonds or ruptures
401 before the sample failure (see Figure 14(c)). A similar response was observed in experimental
402 investigations conducted by Bousselham and Chaallal (2008). It can be concluded that there
403 was virtually no difference between the lightweight samples and their normal weight
404 companions regarding the general trend of the CFRP reinforcement contribution, a similar
405 response was observed for all the tested samples. However, the contribution of CFRP in
406 LWC is slightly lower than the corresponding NWC samples.

407 Table 11 summarises the maximum shear contribution provided by concrete and the CFRP.
408 Interestingly, the CFRP contribution to shear using the subtraction method of analysis is very
409 close to the values when the strain readings are used to evaluate the shear strength component
410 provided by CFRP reinforcement. Hence the additional confinement effect in the presence of
411 CFRP can be neglected based on the subtraction method of analysis.

412

413 Table 11: Maximum shear contribution provided by concrete and the CFRP reinforcement

Sample	Total shear capacity (kN)	Subtraction Method of Analysis (kN)	Shear strength provided by concrete and CFRP reinforcement	
			V_f (kN)	V_c (kN)
BL	151.78	0	0	151.78
BL-UST	218.38	66.6	68.6	149.82
BL-CST	267.14	115.4	118.6	148.53
BN	164.1	0	0	164.1
BN-UST	248.6	84.5	84.1	164.3
BN-CST	320.8	156.7	159.7	161.1

414

415 **COMPARISON WITH DESIGN CODES AND GUIDELINES**

416 Current design codes and guidelines such as ACI 318-08 (2008), CAN/CSA-S6 (2006) and
417 Eurocode2 (2014) present calculations for the shear carrying capacity of normal weight
418 reinforced concrete beams. In order to calculate the shear resistance of lightweight concrete,
419 a reduction factor was proposed. ACI 318-08 suggests to use 0.85 as the reduction factor.
420 Eurocode 2 provides a reduction factor which is related to density of the lightweight concrete.
421 However, the shear prediction of CAN/CSA-S6 includes the density of concrete. Therefore,
422 the density of lightweight concrete could be used for the prediction of shear strength. Shear
423 predictions of normal and lightweight concretes illustrates that the CAN/CSA-S6 are close to
424 experimental results (see Table 12). The predication of ACI 318-08 and Eurocode 2
425 underestimate the shear capacity of the control lightweight and normal weight samples. This
426 may be attributed to the arching effects developed by the low shear span-to-depth ratio
427 ($a/d=2.2$) which increases the shear resistances of the tested samples.

428 Table 12: Experimental and predicted results of control samples

Sample	Experimental result (kN)	ACI 318-08 (kN)	Eurocode 2 (kN)	CAN/CSA-S6 (kN)
BN	164.1	116.6	120.3	164.6
BL	151.8	100.5	100.3	137.9

429

430 Furthermore, ACI 440.2R (2008), TR-55 (2013) and CAN/CSA-S6 (2006) allow the
 431 estimation of the contribution of CFRP separately to the concrete contribution. The
 432 experimental results (using the subtraction method of analysis, from Table 11) and numerical
 433 predictions using the current design codes for the CFRP contribution of the tested LWC and
 434 NWC beams are summarised in Table 13.

435 Table 12: Experimental and predicted results of CFRP shear contribution for strengthened
 436 samples
 437

Sample	CFRP contribution from subtraction method (kN)	ACI 440.2R (kN)	TR-55 (kN)	CAN/CSA-S6 (kN)
BL-UST	66.6	73.6	72.1	71.6
BL-CST	115.4	79.6	79.6	79.6
BN-UST	84.5	73.4	70.2	71.6
BN-CST	156.7	79.6	79.6	79.6

438
 439 The predictions of the ACI 440.2R (2008), TR-55 (2013) and CAN/CSA-S6 (2006)
 440 overestimate the contributions of U-shaped CFRP reinforcement of the LWC retrofitted beam
 441 (BL-UST). These codes use the concrete compressive strength for the prediction of CFRP
 442 contribution. As noticed, the tensile strength and the bond strength between lightweight
 443 concrete and FRP are significantly low compared to normal weight concrete while
 444 compressive strengths are the same. Furthermore, BL-UST has a limited bond length.
 445 Therefore, the prediction of the CFRP contribution on LWC beams using design guidelines
 446 should be modified with available effective length and tensile strength of concrete.

447 **CONCLUSION**

448 This study investigated the efficiency of epoxy-bonded CFRP strips on lightweight concrete
449 in shear. While the normal weight concrete samples agrees with the existing experimental and
450 numerical studies, the following conclusion can be derived on lightweight concrete samples:

- 451 • The shear strength gained due to CFRP reinforcement for lightweight samples is less
452 than the normal weight concrete samples. This is probably attributed to lower concrete
453 surface tensile strength and aggregates interlock.
- 454 • The test observations reveal that there was virtually no difference between the
455 lightweight beams and their normal weight companions regarding the failure modes and
456 shear cracks inclinations. However, it was noticed that the path of diagonal tension
457 cracks on the tested LWC samples propagated through coarse aggregates rather than in
458 the concrete matrix around the aggregates as in normal weight samples. It can be also
459 concluded that the LWC samples had higher cracks width due to lower aggregate
460 interlock at the primary shear crack interface.
- 461 • Samples with Closed-shaped CFRP reinforcement experienced higher CFRP strains
462 compared with U-shaped sample, which failed due to the premature debonding of the
463 CFRP reinforcement from the surface of concrete. Furthermore, numerical predictions
464 using design guidelines and codes overestimate the CFRP contribution in the
465 lightweight concrete beam strengthened with U-shaped CFRP system. This is result of
466 insufficient bond length, which significantly influenced by the tensile strength of
467 lightweight concrete (Al-Allaf et al., 2016).
- 468 • Therefore, the effect of CFRP on lightweight concrete should receive more attention in
469 the current design codes and guidelines, which were derived and verified using
470 experimental results of FRP strengthened system on normal weight concrete. Further

471 analytical and experimental studies are required to include the characteristics of the
472 FRP/ lightweight joints in current codes and guidelines to evaluate the efficiency of
473 using FRP reinforcement to strength LWC structures where the effective bond could not
474 be achieved.

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